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Band gap engineering of In_2O_3 by alloying with Tl_2O_3

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Efficient modulation of the bandgap of In_2O_3 will open up a route to improved electronic properties. We demonstrate using *ab initio* calculations that Tl incorporation into In_2O_3 reduces the band gap and confirm that narrowing of the gap is observed by X-ray photoemission spectroscopy on ceramic surfaces. Incorporation of Tl does not break the symmetry of the allowed optical transitions, meaning that the doped thin films should retain optical transparency in the visible region, in combination with a lowering of the conduction band effective mass. We propose that Tl-doping may be an efficient way to increase the dopability and carrier mobility of In_2O_3 . © 2013 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4860986>]

Transparent conducting oxides (TCOs) are now ubiquitous in modern optoelectronic devices, having applications in solar cells, flat panel displays, smart windows, etc.¹ Sn-doped In_2O_3 ($\text{In}_2\text{O}_3\text{:Sn}$ or ITO), which has an optical band gap of ~ 3.75 eV, is currently the industry standard *n*-type TCO, possessing concomitant carrier concentrations exceeding 10^{21} cm^{-3} , resistivities below 10^{-5} Ω cm, and transparency as high as 90%.² Over the past decade concerns over the availability and abundance of In have resulted in large fluctuations in the cost of In and have spawned a research drive to replace In in TCOs.³ Alternative TCOs, namely, $\text{SnO}_2\text{:F}$ (FTO), $\text{SnO}_2\text{:Sb}$ (ATO), and ZnO:Al (AZO) have all received much attention. However, they have thus far failed to equal the consistent high performance of ITO. Recently, a new perovskite TCO, BaSnO_3 , has emerged as a more earth abundant alternative although investigations into this material are only in their infancy.⁴

The excellent dopability and high performance of In_2O_3 as an *n*-type TCO can be easily understood from an examination of its band structure and its band alignment relative to other TCOs. An ideal *n*-type TCO materials should possess (i) a large optical band gap ensuring that the material is transparent, (ii) the ability to become a degenerate semiconductor when donor doped, (iii) a large separation between the conduction band minimum (CBM) and the next lowest conduction band (CBM+1) ensuring that when donor doped, the system can still remain transparent, and (iv) a small effective mass at the CBM, ensuring good electron mobility. Point (ii) is generally dominated by the position of the CBM relative to the vacuum level, with the greater the distance of the CBM from the vacuum level indicating a greater electron affinity (EA), and thus greater *n*-type dopability.⁵

Until 2008, the fundamental band alignment of In_2O_3 had not been well understood, due to confusion over the exact nature of the fundamental band gap. Walsh *et al.* used a combination of *ab initio* calculations and photoelectron spectroscopy measurements to show that the fundamental band gap of In_2O_3 was not indirect in nature as had been proposed previously.⁶ The fundamental band gap is ~ 0.8 eV smaller than the optical band gap of In_2O_3 , as transitions from states within 0.8 eV of the valence band maximum (VBM) to the conduction band (CB) are symmetry disallowed.^{6,7} This understanding helped to rationalize previous XPS band alignments, which had considered that the CBM of In_2O_3 was 3.75 eV above the VBM. The ability to lower the CBM of In_2O_3 relative to the vacuum level and also to simultaneously decrease the effective mass of the CBM would have a huge effect on its electronic conductivity and also on the ability to modulate the workfunction and open up the material for other applications, such as hole injection layers in organic photovoltaics.

Band gap engineering of semiconductors may be approached in a number of ways, including strain engineering,⁸ inducing lattice disorder,⁹ or chemical doping.¹⁰ To date, however, no reports of the modulation of the band gap of In_2O_3 exceeding ~ 0.1 eV have been reported. In this Letter we propose Tl-doping as an efficient mechanism for lowering the band gap of In_2O_3 . We demonstrate using density functional theory (DFT) and that the fundamental band gap of $\text{In}_{2-x}\text{Tl}_x\text{O}_3$ ($0 < x < 0.125$) can be tuned from ~ 2.75 eV to 2.25 eV. Crucially, the nature of optical transitions are not altered in the doped system, meaning that the optical band gap can be modulated from ~ 3.75 eV to ~ 3.25 eV, maintaining optical transparency for the doped system. High resolution X-ray photoemission measurements provide provisional evidence of narrowing of the fundamental gap at Tl-rich ceramic surfaces of $\text{In}_{1.98}\text{Tl}_{0.02}\text{O}_3$.

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All our DFT calculations were performed using the VASP code,¹¹ with interactions between the cores (In:[Kr], Tl:[Xe], and O:[He]) and the valence electrons described using the Projector Augmented Wave method.¹² The calculations were performed using the HSE06 hybrid functional as proposed by Krukau *et al.*¹³ In the HSE06 approach, a value of exact nonlocal exchange, α , of 25%, and screening parameter of $\omega = 0.11$ bohr⁻¹ are added to the Perdew Burke Ernzerhof (PBE) formalism. The Heyd Scuseria Ernzerhof (HSE) approach has been proven to result in structural and band gap data in better agreement with experiment than standard DFT functionals¹⁴ and, crucially, to provide an excellent description of the electronic structure of both Tl₂O₃ (Ref. 15) and In₂O₃.¹⁶ A plane-wave cutoff of 400 eV and a k -point sampling of Γ -centered $3 \times 3 \times 3$ for the 40 atom primitive cell of Tl₂O₃ and In₂O₃ were used, with the structure deemed to be converged when the forces on all the atoms were less than 0.01 eV Å⁻¹. The optical transition matrix elements and the optical absorption spectrum were calculated within the transversal approximation.¹⁷ Within this methodology, the adsorption spectra is summed over all direct VB to CB transitions and therefore ignores indirect and intraband adsorptions.¹⁸

For comparison with the DFT calculations ceramic sample of In_{1.98}Tl_{0.02}O₃ and In_{1.88}Tl_{0.12}O₃ were prepared by firing mixtures of In₂O₃ and Tl₂O₃ intimately ground in an agate mortar and pestle and pressed into 13 mm diameter pellets under a loading of 5 tonnes. The pellets were enclosed in a blanket of unpressed powder of the same composition to prevent loss of volatile Tl₂O₃ and sintered at a temperature of 600 °C for 24 h in recrystallised alumina crucibles. Owing to the toxicity of Tl and its compounds, the furnace used in this procedure was housed in a fume hood. X-ray photoelectron spectra were measured in a Kratos Axis Ultra delay line detector system using a fixed anode monochromatic Al $K\alpha$ X-ray source operating at 120 W and 125 mm mean radius spherical sector analyser. Data were collected with a pass energy of 40 eV for the high resolution scans. The nominal energy resolution was around 0.50 eV. The system was operated in the hybrid mode, using a combination of magnetic immersion and electrostatic lenses with spectra acquired over an area approximately $300 \times 700 \mu\text{m}^2$. A magnetically confined charge compensation system was used to minimize charging of the sample surface, and all spectra were taken with a 90° take off angle. The resulting spectra were referenced to a weak Fermi edge observed in the spectra. There was evidence of pronounced segregation of Tl to the near surface region of the pellets with a surface Tl/(In + Tl) ratio of 0.19 (i.e., an effective x values of 0.38 where x is defined by the formula In_{2- x} Tl _{x} O₃) as gauged by Tl 4 f and In 3 d intensities (after correction with atomic sensitivity factors supplied by the instrument manufacturer) for the sample with a nominal bulk x values of 0.02. The surface Tl content for the sample with $x = 0.12$ was 0.72. The concentration of Tl in the near surface region as probed by XPS is therefore significantly greater than the bulk Tl levels of $x = 0.125$ and $x = 0.25$ treated in the calculations even at the very low bulk x values of the two samples studied in the experiments.

The stable oxides of In and Tl are the sesquioxides (In/Tl)₂O₃, which both crystalize in the cubic bixbyite (FeMnO₃) structure, with 40 atoms (8 f.u.) in the primitive

unit cell, and 80 atoms in the conventional cell. All oxygen sites in this structure are equivalent, coordinated to four cations, whereas there are two distinct cation sites (8 b and 24 d in Wyckoff notation) which are each coordinated to 6 anions in a distorted octahedra. One quarter of all the cations occupy the 8 b position, with the remaining three quarters occupying the 24 d positions. Our calculated lattice constants for In₂O₃ and Tl₂O₃ are 10.16 Å and 10.56 Å, which are within 0.40% and 0.02% of the experimental lattice constants respectively. The calculated band gaps at the HSE06 level are 2.75 eV and 0.33 eV for In₂O₃ and Tl₂O₃, respectively, in good agreement with experimental measurements.

We have tested the incorporation of one Tl into the 40 atom primitive cell of In₂O₃ (i.e., replacing 6.25% of the In atoms) on both the 8 b and 24 d sites. Tl is 0.045 eV more stable on the 24 d site, indicating that it will have a small preference at room temperature for taking up this site. We have also tested whether Tl ions will cluster when doped into In₂O₃, by calculating different combinations of dopant ordering in an 80 atom unit cell. This analysis reveals that there is a 2 meV preference for Tl ions to sit on neighbouring 24 d sites, meaning that there is not a large thermodynamic driving force for Tl clustering.

The HSE06 calculated band structures for In₂O₃, In_{1.875}Tl_{0.125}O₃, In_{1.75}Tl_{0.25}O₃, and Tl₂O₃ are shown in Figure 1. It is immediately obvious that the incorporation of Tl causes the band gap to decrease. This is not unexpected as the band gap of isoelectronic and isostructural Tl₂O₃ is only 0.35 eV, due to in large part to very pronounced relativistic stabilisation of the Tl 6 s states.¹⁹ The CBM effective masses for In₂O₃, In_{1.875}Tl_{0.125}O₃, In_{1.75}Tl_{0.25}O₃, and Tl₂O₃ were calculated to be 0.30, 0.29, 0.27, and 0.22 m_e , respectively, indicating that the inclusion of Tl also lowers the effective mass, and should promote higher electron mobility.

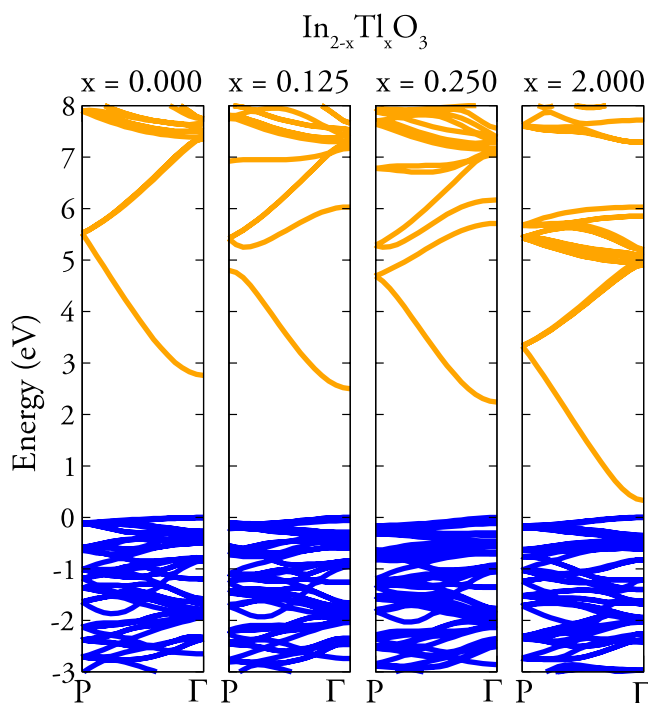


FIG. 1. Band structure of In_{2- x} Tl _{x} O₃ for $x = 0.000, 0.125, 0.250,$ and 2.000 . Blue and orange denote valence bands and conduction bands. The VBM is set to 0 eV in each case.

A simple band alignment derived from a charge neutrality level (CNL, or branch point energy) approach²⁰ is displayed in Figure 2. This approximate model places the ionization potential of In_2O_3 at 7.81 eV, which is in good agreement with recent calculated²¹ and experimental measurements.²² It is clear that the incorporation of Tl lowers the position of the CBM relative to the vacuum level, necessarily increasing the distance that the CNL is above the CBM. This result indicates that Tl-doped In_2O_3 should be easier to dope *n*-type and opens up the possibility that oxygen vacancies, which are the dominant intrinsic defect in In_2O_3 and Tl_2O_3 , might transition from being relatively deep donors in bulk In_2O_3 (Ref. 23) towards being fully ionized as they are in Tl_2O_3 .¹⁵

As we have now established that Tl incorporation decreases the fundamental band gap of In_2O_3 , it is instructive to investigate how Tl incorporation affects the optical band gap. Both In_2O_3 and Tl_2O_3 possess symmetry disallowed transitions from states within ~ 0.8 eV and ~ 1.2 eV, respectively, of the VBM to the CBM, meaning that their optical band gap is considerably larger than their fundamental band gap. The HSE06 calculated optical absorption spectra for In_2O_3 , $\text{In}_{1.875}\text{Tl}_{0.125}\text{O}_3$, and $\text{In}_{1.75}\text{Tl}_{0.25}\text{O}_3$ are displayed in Figure 3. Tl-doping up to 12.5% does not affect allowed transitions from VB to CB, meaning that even with a reduced fundamental band gap, the optical band gap remains larger than the threshold for optical transparency of 3.1 eV. This indicates that although the CBM has been lowered, increasing the *n*-type dopability, the doped material is still a TCO.

Very provisional experimental verification of these ideas is provided by the valence band X-ray photoemission spectra shown in Figure 4. For nominally undoped In_2O_3 the onset of the valence band edge is about 2.88 eV below the surface Fermi level, as has been found previously.^{6,24} The position of the valence band edge is influenced by a number of factors including experimental spectral broadening²⁵ and band bending at the surface, leading for undoped In_2O_3 to formation of

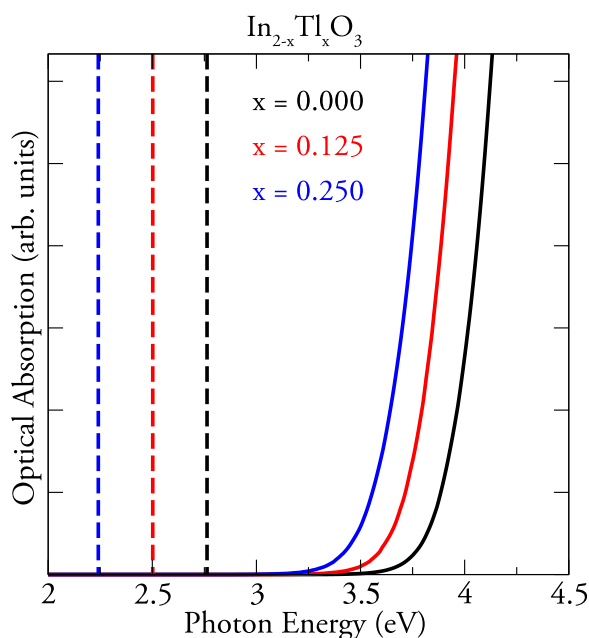


FIG. 2. HSE06 calculated optical absorption spectra for $\text{In}_{2-x}\text{Tl}_x\text{O}_3$ for $x=0.000, 0.125,$ and 0.250 . Dashed lines indicate fundamental band gap, and full lines indicate optical absorption.

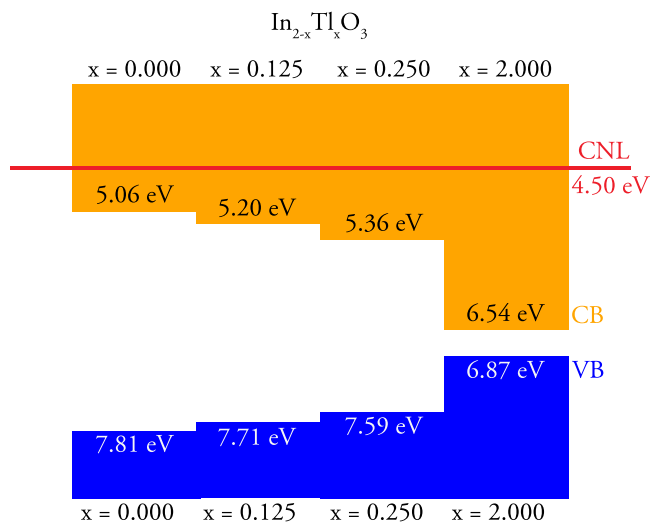


FIG. 3. Band alignment of $\text{In}_{2-x}\text{Tl}_x\text{O}_3$ for $x=0.000, 0.125, 0.250,$ and 2.000 calculated using the CNL alignment method. All energies are given relative to the vacuum level, using the assumption that the CNL sits at ~ 4.5 eV below the vacuum level.²⁰

an electron accumulation layer.⁷ Despite these complications *changes* in the position of the valence band edge upon alloying with Tl can be regarded as significant. It is therefore interesting to find that the valence band edge moves to lower binding energy with incorporation of Tl, with an onset at 2.49 eV for a surface *x* value 0.36. Since binding energies are referenced relative to the Fermi energy, which lies close to the CBM, this indicates narrowing of the bandgap in the

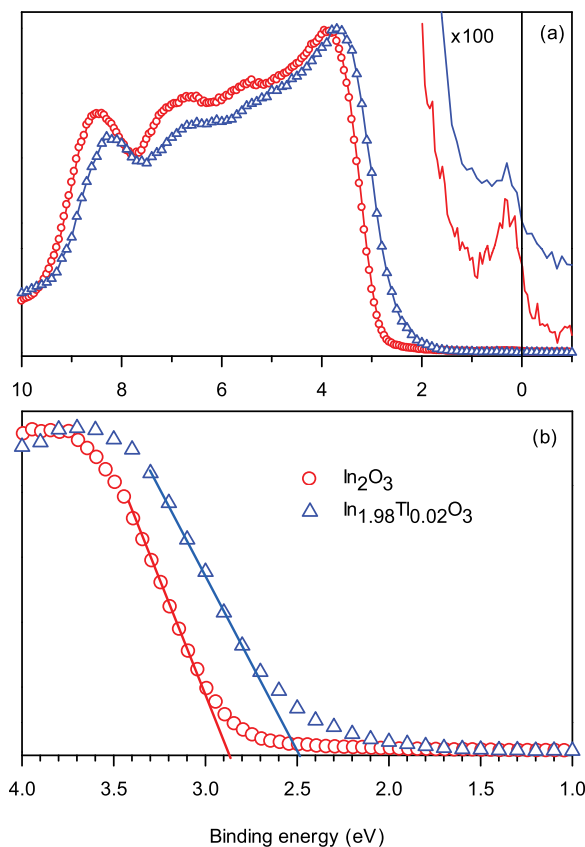


FIG. 4. (a) Valence band photoemission spectra of undoped In_2O_3 and a samples with nominal bulk composition $\text{In}_{1.98}\text{Tl}_{0.02}\text{O}_3$. (b) Expanded views of the low binding energy region showing the linear extrapolation procedure used to define the position of the valence band edge.

surface region probed by XPS assuming that there is no change in the band bending. Somewhat surprisingly however the intensity of the emission from conduction band states close to the Fermi energy decreases slightly with increasing Tl doping. In fact for a sample with nominal bulk composition $\text{In}_{1.88}\text{Tl}_{0.12}\text{O}_3$ it was not possible to locate the Fermi edge with any confidence. Coupled with the very pronounced surface segregation of Tl found for both samples, these observations suggest that Tl may be partly accommodated at the surface as Tl^{+} : the propensity of lone pair cations of this sort to segregate to surface sites is well documented.^{26,27} The Tl^{+} would effectively act a two electron acceptor, partly compensating the charge carriers arising from oxygen vacancies or other native donor defects. Compensation of this sort has been found in Bi-doped PbO_2 , where Bi acts as an acceptor rather than as a donor. In the formally related system Sb-doped SnO_2 the Sb acts as a donor, as expected from simple electron counting considerations.^{27,28} Support for the idea of accommodation of a fraction of the Tl in surface sites as Tl^{+} is provided by the observation that the intensity of photoemission in the bandgap region immediately above the extrapolated valence band edge is stronger in the alloy samples than in undoped In_2O_3 : this is where the antibonding lone pair states are expected.

Overall then it must be acknowledged that even though XPS provides tantalising evidence of bandgap narrowing in $\text{In}_{2-x}\text{Tl}_x\text{O}_3$, the experimental work does highlight obvious difficulty in incorporating Tl in the bulk of In_2O_3 and also suggests that Tl may act to compensate native donors when it segregates to the surface. However the results are sufficiently encouraging to warrant investigation of deposition of $\text{In}_{2-x}\text{Tl}_x\text{O}_3$ thin films although several safety issues need to be resolved before we can embark on this work.

Hybrid DFT calculations combined with high resolution XPS measurements have demonstrated that Tl incorporation into In_2O_3 can lead to a significant reduction in the band gap, arising from pronounced stabilisation of the CBM relative to the vacuum level. Concomitant lowering of the effective mass at the conduction band edge is predicted by the calculations, whilst maintaining optical transparency in the visible region. This effect should in principle make In_2O_3 :Tl a more efficient *n*-type TCO even than In_2O_3 . At the same time lowering of the CBM relative to the vacuum level will lead to an increase in the work function provided the Fermi level stays close to the CBM, as is found experimentally in the present work. This could lead to improved hole injection in organic light emitting diodes. These issues all warrant further experimental investigation, although difficulty in incorporating Tl into the bulk of In_2O_3 may well prove to be problematic.

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