

Meeting QoS Requirements in a Dynamically Priced Commercial Cellular Network

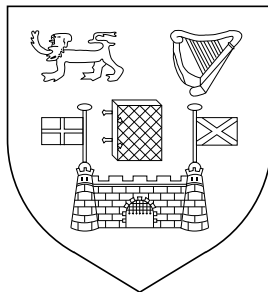
by

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Declaration

I declare that the work described in this dissertation is, except where otherwise stated, entirely my own work and has not been submitted as an exercise for a degree at this or any other university.

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Abstract

With the current trend towards user mobility and ubiquitous computing, cellular networks are becoming an evermore important feature of day-to-day life, albeit an unseen one. Mobile networks are characterised by a scarcity of resources, particularly bandwidth and frequency spectrum. However, for new multimedia applications, such as video telephony, a large amount of these resources is required and, moreover, these applications demand that specific quality of service guarantees are met by the network at all times.

In a cellular network, the traffic is highly variable both temporally and spatially. Therefore, dimensioning a network so that it can meet peak-time demand is both uneconomic and inefficient, as most of the time the network will be under-utilised. This leads to frequent and significant congestion in mobile networks, so that, at a certain time and place, users may find it impossible to start a phone call, or an ongoing phone call may be interrupted. Some solutions have been proposed to alleviate the problem of congestion without installing new infrastructure. However, these schemes only improve the network performance for some incoming traffic rates, but cannot meet QoS guarantees at peak-times.

Another possible solution to this problem is to attempt to modify the user demand to fit the available resource. This leads to dynamic pricing: charging users according to the current traffic conditions, hence providing negative or positive incentives to regulate the traffic entering the network. As they know the price they will be charged, users can decide whether to make the phone call or not, and the importance of the call will influence their choice. Hence dynamic pricing leads to a natural prioritisation of calls, ensuring that only low priority calls are blocked.

Dynamic pricing has been applied successfully in several domains, but its application to cellular networks is an emerging research area and is particularly challenging due to the mobility of users. This project investigates dynamic pricing in cellular networks from a technical perspective. For this purpose, detailed network and traffic models are defined based on an investigation of current research in related areas. These models are implemented in a simulator which is then used to test, refine and improve existing dynamic pricing schemes for both GSM and GSM/GPRS networks.

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Chapter 1

Introduction

1.1 Context

With the current trend towards mobile and ubiquitous computing, cellular networks are becoming an evermore important feature of day-to-day life, albeit an unseen one. Mobile networks are characterised by a scarcity of resources, particularly bandwidth and frequency spectrum. However, many new multimedia applications such as video telephony have specific resource requirements and demand that tight quality of service guarantees are met by the network at all times.

To compound the problem, demand on a cellular network differs significantly between peak and off-peak times [29]. This means that dimensioning a network so that peak hour demand may be met is both uneconomic and inefficient, as the network capacity will be under-utilised most of the time. Moreover, the mobility of users in a cellular network can cause unexpected geographical congestion due to clustering in unexpected areas. These limitations mean that during times of peak demand, network operators cannot accept all calls while still meeting their users' quality of service (QoS) requirements.

The first possible solution to this problem is to increase the network capacity. Cell splitting and frequency re-use may be used for this purpose. This results in a higher cell density, hence urban areas now have far more cells per square kilometre than rural ones, but this is expensive and will increase the overhead due to hand-off calls. Some other solutions to alleviate the congestion problem that do not require installation of new infrastructure have been proposed. In GSM/GPRS networks, a degree of flexibility in the number of available channels per cell may be achieved by moving capacity between cells (dynamic channel assignment) or by using the overlap between cells and allocating calls to cells according to the level of traffic in each cell (alternate routing) [14, 27]. The main disadvantages of

such dynamic capacity allocation techniques are the increased computational load on the system and the increase in co-channel interference. In UMTS, an adaptative cell-sizing algorithm has been suggested as a means of relieving congestion [44]. However, this approach fails when traffic is uniform i.e. when in a cell cluster, all cells are busy at the same time. In recent years, considerable efforts have focused on Call Admission Control (CAC). The goal of a CAC scheme is to decide whether or not to accept a call request. Its purpose is to maximise the utilisation of resources while still providing the required QoS for all calls.

An alternative approach to the network utilisation problem is to attempt to modify the user demand to fit the available resource. Mobile network users act “selfishly”: as there is no notion of “community”, users have no reason to take into account the existence of other users. Therefore, the only possible incentive on the demand is the price. Currently, most mobile service providers offer cheaper off-peak calls as a marketing incentive, in an attempt to utilise spare network capacity. However a major drawback of this scheme is its lack of flexibility and inability to take into account the actual network load, by merely increasing the tariff when the operator anticipates high demand. A better solution is to provide a negative or positive incentive according to current traffic conditions. This approach leads to dynamic pricing, that is, the price is adjusted dynamically based on prevailing network conditions. One of the possible implementations is that, users would be told the price per time unit for a call as they are about to make it. This pricing scheme is designed to regulate the incoming call rate, as some users will decide not to make a phone call if the price is too high.

As the traffic in cellular networks is highly variable in both space and time, the number of users willing to make a phone call may be instantaneously very high, thus leading to a very high price. A certain proportion of connection attempts made during the busy period and suppressed due to the very high price will never be made again. This may represent lost revenue for the service provider, however this must be compared with the proportion of calls lost due to call blocking and call dropping. Users may choose whether to proceed with a call or not and the importance of the call will influence their decision. Therefore dynamic pricing allows a natural prioritisation of the calls to occur, ensuring than only low priority calls are lost. This is an improvement on the current system, where calls are lost indiscriminately [9].

1.2 Project Goal

The goal of the work described below is to investigate dynamic pricing in cellular networks. Dynamic pricing in cellular networks is an emergent field and only a few studies have been conducted in this area. Existing work focuses mainly on economical studies of the consequences of dynamic pricing

(modelling user reaction to changes in price and QoS) and sometimes technical details may have been neglected. Furthermore, many aspects of cellular networks have yet to be fully investigated; this includes the use and design of CAC schemes and the specifications of some protocols. For example, there is on-going work on the resource assignment for GPRS/GSM networks: how are the resource shared between GPRS and GSM calls? (see [35] for example). Should a GPRS session be allocated several channels if required? Should some or all of these channels be released if their is no channels available for voice calls? [7]. This on-going work on the specification of cellular networks means that it is particularly difficult to create an accurate model of existing and future cellular networks.

This work seeks to define a model of existing and emerging networks that is as accurate as possible by surveying the related literature. This model will be then used to test and enhance existing pricing policies.

1.3 Contribution to Knowledge

This work presents a model for a GSM/GPRS networks, which includes provision for hand-off calls, CAC and detailed traffic descriptions. A simplified version of this model has been studied analytically to explore the behaviour of existing pricing schemes in this environment. This has been studied in more detail through simulation where several aspects of these networks have been explored. The contribution of this work is threefold: the definition of a model of existing and emergent cellular networks, the creation of a simulator which implements this accurate model and, hence, is a powerful tool for studying pricing policies and the exploration of improvements to existing pricing schemes.

1.4 Dissertation Outline

In the following chapter, recent research work in fields related to cellular networks and, in particular pricing in cellular networks, is reviewed. The achievements and limitations of each of these studies is outlined. The network model designed by taken into account existing work, is presented in chapter 3. In the subsequent chapter, a mathematical analysis of a simplified model of the network and traffic is detailed and its limitations highlighted. This work clearly demonstrates the need for an accurate network simulator. The simulator specifically written to explore dynamic pricing is described in chapter 5. Finally, the experiments carried out using this simulator and the results obtained are presented in chapter 6.

Chapter 2

State Of the Art

In this chapter, we briefly review different Call Admission Control schemes proposed in the literature, discussing the performance and possible deficiencies of each scheme. To improve congestion avoidance, dynamic pricing may be introduced alongside Call Admission Control. Dynamic pricing in cellular networks is an emergent research domain. Relatively few theoretical studies [13, 21, 47] have been conducted in this area and even fewer empirical studies have been performed. A detailed review of the existing work on dynamic pricing in cellular network is provided in section 2.2. Dynamic pricing has already been studied and implemented in other research domains: we draw on the conclusions of these studies and try to identify how they may be used to improve work on dynamic pricing in mobile networks in section 2.3.

2.1 Call Admission Control Schemes

The negative effects of congestion in cellular networks are experienced by mobile users everyday: when a network is congested, the system cannot admit all calls, hence calls may be refused entry to the network or interrupted while in progress. It is estimated that, with the development of next generation networks, congestion will occur more often due to an increase in traffic that is attributed to an increase in data transmission. To alleviate this problem, different Call Admission Control (CAC) schemes have been proposed. A Call Admission Control scheme is a provisioning strategy used to limit the number of calls connected to a network in order to reduce network congestion and provide a desired Quality Of Service (QoS) to users in the system [21]. These are particularly difficult to design in the case of cellular systems because of the mobility of users: a user can start a call in one cell and roam to another cell, while the call is still in progress. In this case the call needs

to be handed off to the other cell, and will require the allocation of sufficient bandwidth in the cell it roams into. Hence a call can either be *blocked*: a bandwidth request for a new call in a congested cell is not granted, resulting in the call not being able to start, or *dropped*: a call is interrupted during its execution because the user roamed to a cell which doesn't have sufficient available bandwidth. As users are more sensitive to call dropping (when a conversation is interrupted) than to call blocking (when a call cannot be made), most CAC schemes try to give hand-off calls priority over new calls. As explained in [21], various hand-off priority-based CAC schemes have been proposed in the literature and these may be roughly classified into three categories:

1. Guard Channel Schemes: A number of channels in each cell are reserved for exclusive use by hand-off calls; the remaining channels are shared by both new and hand-off calls [16, 18, 19, 28];
2. Queueing Priority Schemes: When all channels are occupied, either new calls are queued while hand-off calls are blocked [30] or new calls are blocked while hand-off calls are queued [45] or both calls are queued [5];
3. Channel Borrowing Schemes: When all the channels in a cell are occupied, the cell borrows channels from other cells to accommodate the incoming hand-off calls [6].

Within a certain range of call arrival rates, these schemes can improve system performance. However, it has been observed [21] that, with the increase of call arrival rate, both the new call blocking probability and the hand-off call blocking probability increase. When the call arrival rate is temporarily very high (for example at peak times), no matter how the parameters are adjusted, these schemes cannot guarantee a specified QoS to users. One solution to this problem is to introduce dynamic pricing on the network.

2.2 Dynamic Pricing in Cellular Networks

Two main studies of dynamic pricing in cellular networks have been identified. The first [12, 9, 13, 10, 11] conducted by Fitkov-Norris and Khanifar, proposes a pricing scheme for GSM/GPRS networks. The second [20, 21], by Hou, Yang and Papavassiliou, aims to introduce schemes which combine dynamic pricing and CAC. These two studies are detailed below, together with a brief overview of other work in this area. We begin with a discussion on two fundamentally different approaches to dynamic pricing in mobile networks.

2.2.1 Network Use Maximisation vs. Operator Revenue Optimisation

There are two fundamentally different approaches to dynamic pricing; the first one explored considered wireless resources as a public good. In this case, the system aims to ensure that the network is efficiently used, hence maximising the welfare of the consumers. In term of economics, *utility functions* describe users' level of satisfaction with the perceived quality of service [24], that is, they characterise how sensitive users are to the changes in QoS. The higher the utility, the more satisfied the users are. To maximise the use of the network as a public good, the total user utility (the sum of each individual users utility) should be maximised [24]. This approach leads to users being charged marginal prices, that is the direct cost of the call to the operator.

A second approach is to maximise network operator revenue. As the network operator sets the pricing scheme, it is expected that this approach will be more widely used. Furthermore, it has been estimated that marginal cost pricing does not adequately cover the set up and running costs of the network operator [25]. Therefore, implementing these charging techniques could lead to reduction of profitability: the ratio between the amount of capital which is invested into the network (investment) and the income from it must be such that the basic interest rate on the investment and the expected profit will be met [48].

It should be noticed than while these are two fundamentally opposing approaches, a third approach would be to maximise some combination of the total users utility and the operator revenue, hence leading to a possible compromise between these two goals.

2.2.2 A Self-Regulated Dynamic Pricing Algorithm for GSM and GPRS

2.2.2.1 Description

A simple dynamic pricing algorithm is presented in [12]. The system is self-regulated and its behaviour over time is determined by the price charged for each phone call (see figure 2.1). The goal of this algorithm is to maximise both the revenue for the service operator and the welfare of the users, that is, to choose the pricing function which offers the best utilisation of system capacity whilst keeping the call blocking probability at a preset level.

At regular intervals, the system calculates a certain number of operational parameters which determine the network utilisation and performance. These parameters are then compared to a set of theoretically estimated target values and a decision is reached as to whether a price adjustment needs to be made. If required, a negative or positive tariff change is calculated, and the price is adjusted accordingly.

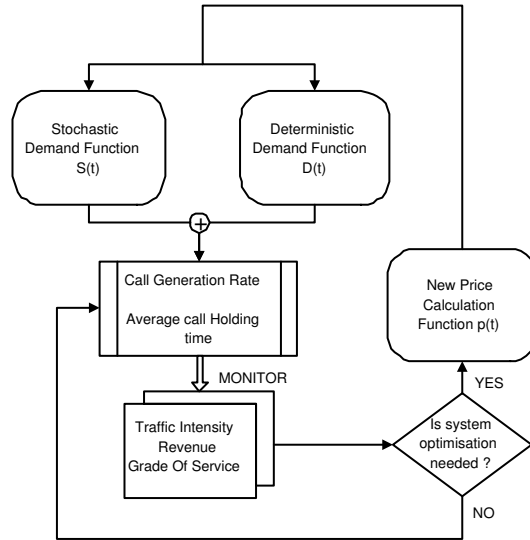


Figure 2.1: Fitkov-Norris and Khanifar algorithm

In [11], Fitkov-Norris and Khanifar present a more complex algorithm which provides for the inclusion of GPRS traffic on the network (c.f. figure 2.2). A function that maps the network load to the price to be charged is introduced. This is characterised by the divergence, M , of the price curve from the straight line connecting the minimum and maximum prices. Increasing M will lead to lower intermediate dynamic prices and reduce the operator revenue, hence M may be interpreted as an index measuring the welfare of users.

2.2.2.2 Implementation

In the case of GSM networks, Fitkov-Norris and Khanifar propose to implement their algorithm in the Base Station Controller (BSC). The availability of the necessary data and of spare computational power make it efficient to compute the price at the BSC; moreover it would minimise the increase of control traffic in the network.

In UMTS networks, channels cannot be explicitly defined, and it is argued that a possible implementation of the algorithm would be to charge users on the basis of the interference they cause to other users. This is known as shadow pricing. In this case, the price charged by the network provider would be proportional to the total number of users in the network and the amount of bandwidth used by each user.

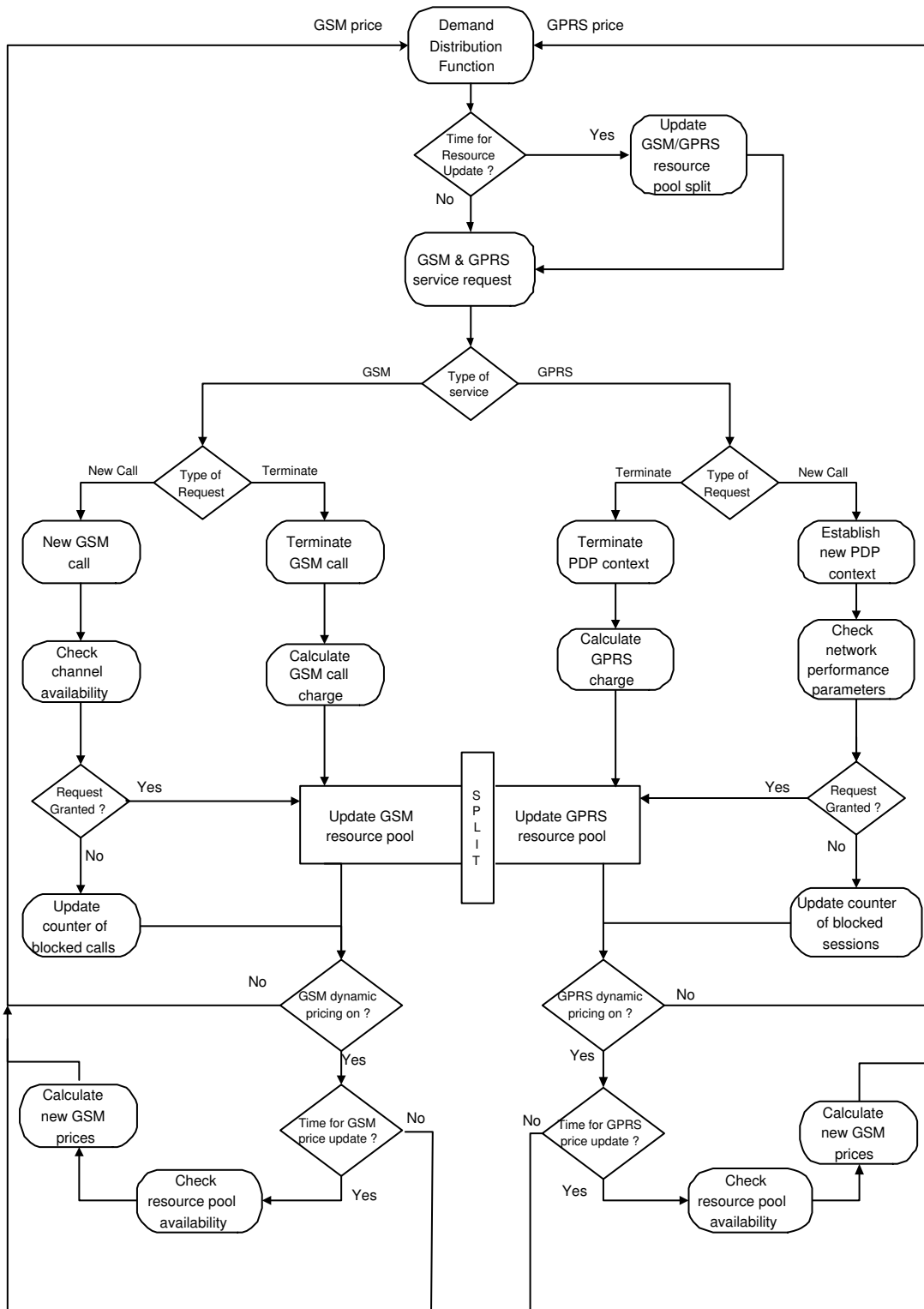


Figure 2.2: Fitkov-Norris and Khanifar GPRS detailed algorithm

2.2.2.3 Demand modelling

The user demand is modelled as a combination of a deterministic function $D(t)$, a function of the time of day which can be predicted fairly accurately, and a random demand $S(t)$ caused, for example, by emergencies. Depending of the price elasticity of demand, a certain number of calls will be generated. It is also assumed that the user holding time is inversely proportional to the price charged by the network.

User Behaviour Model It is expected that mobile network users will change their demand for network resources in response to tariff changes both in terms of the number of connections requested and the average call holding time (connection length) [12]. These two, correlated, effects of dynamic pricing are said to facilitate the convergence of the state of the system to a desired state.

Effect of price on Demand The effect of price on demand is modelled using an exponential function :

$$Q_X = Ae^{-\beta \cdot P_{Q_X}} \quad (2.1)$$

where

- Q_X is the quantity demanded of good X,
- P_{Q_X} is the price of good X,
- A is the demand shift constant,
- β is the demand elasticity coefficient.

This model is particularly attractive because the elasticity of the demand can be parameterised and depends only of the price of the calls [34]. The demand shift constant A will incorporate the change in demand due to the effect of the time of day using historical data and is therefore time-dependent. To take existing pricing schemes into account, the model is corrected by taking the difference between the peak or off-peak price P_{bias} in the real system and the dynamic price $P_{dynamic}$ in the modelled system. Therefore, the basic demand model may be expressed as:

$$Q_X = A(t)e^{-\beta \cdot (P_{bias} - P_{dynamic})} \quad (2.2)$$

Effect of price on User Mobility Fitkov-Norris and Khanifar used the gravity model to represent the effect of price on user mobility. This model was originally used by Wilson [49], to determine the most probable distribution of the number of trips between two regions depending on the attractiveness of the destinations. It has been adapted to predict the number of calls generated between two cells in a mobile network.

The analogous call gravity model is:

$$\Psi_{ij} = \kappa N_i N_j \left(\frac{1}{p_{ij}} \right) \quad (2.3)$$

where :

- Ψ_{ij} is the total number of calls between cells i and j,
- κ is a constant,
- p_{ij} is the price of the calls between cells i and j,
- N_i is the total number of users in cell i.

To ensure that if the number of users in the cells doubles then the number of calls between the cells does not quadruple, some corrective constants A_i and B_j are introduced. The resulting model, taking into account the pricing bias in the historic demand, is, hence, for an exponential cost function:

$$\Psi_{ij} = A_i B_j N_i N_j e^{-\alpha(p_{ij} - p_{static})} \quad (2.4)$$

with

$$A_i = \frac{1}{\sum_j B_j N_j e^{-\alpha(p_{ij} - p_{static})}} \text{ and } B_j = \frac{1}{\sum_i A_i N_i e^{-\alpha(p_{ij} - p_{static})}}$$

where

- α is an elasticity factor,
- p_{static} is the price before introduction of dynamic pricing.

After simplification [13], the model becomes :

$$\Psi_{ij} = A_i N_i^2 e^{-\alpha(p_{ij} - p_{static})} \quad (2.5)$$

with $A_i = \frac{1}{\sum_j N_j e^{-\alpha(P_{ij} - P_{static})}}$.

Fixed Line Substitution Effect This effect comes into force if the dynamic price of the calls becomes less than the historic off-peak price. Equation 2.2 becomes:

$$D_{Q_x} = A(t)e^{-\beta.(P_{bias} - P_{dynamic})} + E(P_{bias} - P_{dynamic})^{-\beta} \quad (2.6)$$

2.2.2.4 Pricing

Price Update In [12], operational system parameters such as traffic intensity (E_p), revenue (R_p) and Grade of Service (GoS) (ν_p) which determine the network utilisation and performance are calculated and compared to a set of target system performance parameters which have been estimated theoretically. A decision is then reached as to whether an adjustment to the tariff is necessary.

The rate of change of the price for the calls determines the degree of demand regulation in the network [11].

Price Setting In [9, 13], two pricing functions, linear and non-linear are examined. In the former case, the price is linearly proportional to the number of available channels, while in the latter case the relationship is exponential.

In [11], a more complex pricing function is introduced. This is the solution of the following minimisation problem:

$$\begin{aligned} & \text{Min} \left(\int_0^{Q_{max}} (P_{min} + P(q))dq \right) \\ & \text{subject to } \sqrt{1 + P(q)^2}dq = M \end{aligned}$$

where

- q is the load of the network
- M is the divergence of the price curve from the straight line connecting the maximum and minimum price.

The solution is of the form:

$$P(q) = K - P_{min} - \sqrt{\lambda^2 - (h - q)^2}$$

2.2.2.5 Results

This algorithm has been evaluated through simulation [9]. Simulations using both linear and non-linear pricing functions have been carried out and it has been concluded that dynamic pricing leads to a significant improvement in the service provider revenue for both types of pricing functions. However the shape of the pricing function has a significant influence on the total number of blocked calls in the system. It has been noted that the variation of the generation rate and the resulting blocked calls in the system are higher for linear pricing functions. The simulation shows an overall reduction in blocked calls of up to 30%.

2.2.2.6 Further work

In [10], a pricing scheme that maximises the operator revenue is presented. The revenue optimisation problem may be simplified by dividing the total optimisation period into smaller intervals and maximising the revenue over each individual interval. The subintervals will be chosen as the length of time over which the demand time shift constant, $A(t)$, is constant in time. This leads to the following pricing scheme:

$$P_{optimal} = \frac{1}{\beta} \quad (2.7)$$

where β is the demand elasticity coefficient of the demand (see section 2.2).

However, this requires a detailed knowledge of the elasticity of the demand (i.e. the aggregate demand of individual users in the network) and, as such, is not very practical to implement. Furthermore, with this approach, only the network operator revenue is maximised, without maximising the network usage (total number of successful calls in the network). It is suggested that a requirement for attaining a pre-set revenue can be used instead of the maximisation, and in this case the network usage can be maximised (i.e. it can be ensured that the network is always fully utilised).

An analytical definition of the price which ensures that the capacity is fully utilised without call blocking, thus offering satisfactory QoS to the users, is given in [10], but in this case the network operator revenue is not taken into account:

$$P_{dynamic} = \frac{\ln(C + Q(\frac{1-\tau}{\tau})/A(t))}{\beta} + P_{bias} \quad (2.8)$$

where:

- C is the capacity of the network,

- $Q(t)$ is the instantaneous load,
- τ is the user call holding time,
- $A(t)$ is the demand time shift constant,
- β is the demand elasticity coefficient,
- P_{bias} is the price already present in the system.

Simulations to compare the two pricing strategies (equations 2.7 and 2.8) have been carried out and it has been concluded that the revenue generated using the revenue maximisation strategy is significantly higher than that generated using the existing strategy. Moreover, the revenue generated using the utilisation maximising strategy is significantly lower than for both the other strategies. Furthermore, the capacity utilisation pricing strategy is not as effective as the revenue maximisation strategy in keeping the number of blocked calls down. These results suggest that there is a trade-off between the effectiveness of dynamic pricing for revenue maximisation and efficient network utilisation.

2.2.3 Integration of Dynamic Pricing with C.A.C.

The main contribution of Hou, Yang and Papavassiliou is to integrate dynamic pricing with Call Admissions Control schemes [21, 20, 19, 18].

2.2.3.1 Description

In [20], a wireless network that uses a Guard Channel CAC scheme is considered. The arrival of new calls is modelled with a Poisson process and the channel holding time is assumed to follow a negative exponential distribution. Under some further assumptions on the utility function of a single user, it is proved that there exists an optimal new call arrival rate, λ_n^* , which maximises the total utility of users. Furthermore, for this value the channel resources are most efficiently used. When the new call arrival rate $\lambda_n < \lambda_n^*$, users can obtain a better QoS than that specified by their QoS requirements, but some channels resources are wasted. When $\lambda_n > \lambda_n^*$, both the total user utility and the QoS decrease with any further increase of λ_n , that is the cell is congested. From the point of view of guaranteeing QoS, it is preferable for a system to operate with $\lambda_n < \lambda_n^*$.

A system composed of two functional blocks, a Pricing block and CAC block, is introduced. When the traffic load is less than the optimal value, λ_n^* , a normal (fixed) price is charged to the user. If the traffic load increases beyond the optimal value, a dynamic peak hour price depending on current traffic conditions is charged to users.

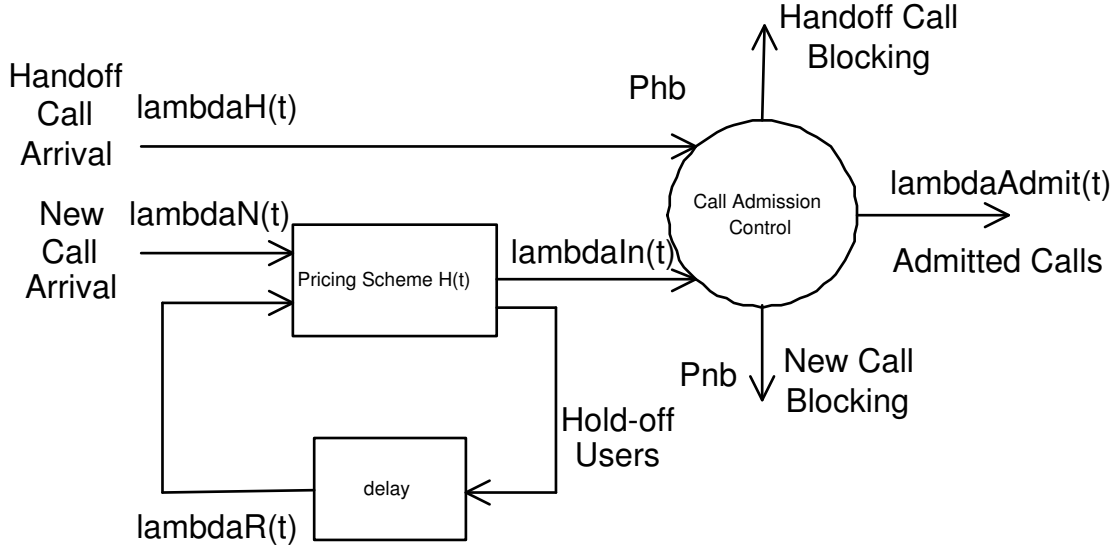


Figure 2.3: Hou, Yang and Papavassiliou's algorithm

2.2.3.2 Demand modelling

User Behaviour model The following demand function is used:

$$D[p(t)] = e^{-\left(\frac{p(t)}{p_0} - 1\right)^2} \quad (2.9)$$

where:

- p_0 is the normal price,
- $p(t)$ is the price charged to users starting calls at time t .

The call incoming rate to the CAC block is

$$\lambda_{in}(t) = D[p(t)] \cdot (\lambda_n(t) + \lambda_r(t)) \quad (2.10)$$

where $\lambda_r(t)$ is the arrival rate of users who have found the price too high and retry after waiting for a while (hold-off users).

2.2.3.3 Pricing

Combining equation 2.9 and 2.10, and using the condition $\lambda_{in}(t) \leq \lambda_n^*$, gives:

$$p(t) = D^{-1} \left(\min \left(\frac{\lambda_n^*}{\lambda_n(t) + \lambda_r(t)}, 1 \right) \right) \quad (2.11)$$

This is the price that should be set at time t in order to obtain the desired QoS.

2.2.3.4 Results

The algorithm has been evaluated by simulation [21]. Five experiments were carried out, depending on the users behaviour (whether after a call being blocked or dropped they retry or not) and on use of the proposed integrated pricing scheme. The five experiments were as follows:

Conventional System with Retry (CSwR): No pricing block was implemented. Users blocked by CAC retry after waiting some time.

Conventional System with Retry and Loss (CSwRL): No pricing block was implemented. One third of the blocked users leaves the system and the rest wait and retry.

Pricing System with Hold-off Retry (PSwHR): The pricing scheme was implemented. A user that does not accept the current price (hold-off user) waits for some time and retries, while blocked users leave the system.

Pricing System with Retry (PSwR): Both hold-off and blocked users retry after waiting some time.

Pricing System with Retry and Loss (PSwRL): One third of the hold-off users and one third of blocked users leave the system, while other users wait some time and retry.

It was observed that the proposed integrated scheme reduces the occurrence of system congestion and meets the users' QoS requirements, while other, conventional, CAC schemes fail to do so. Moreover, considerable improvements are also observed in both the total user utility achieved and the revenue obtained.

2.2.4 Other Work

Dynamic pricing in cellular networks has also been considered by Viterbo and Chiasserini [46, 47], and Wallenius and Hamalainen [48].

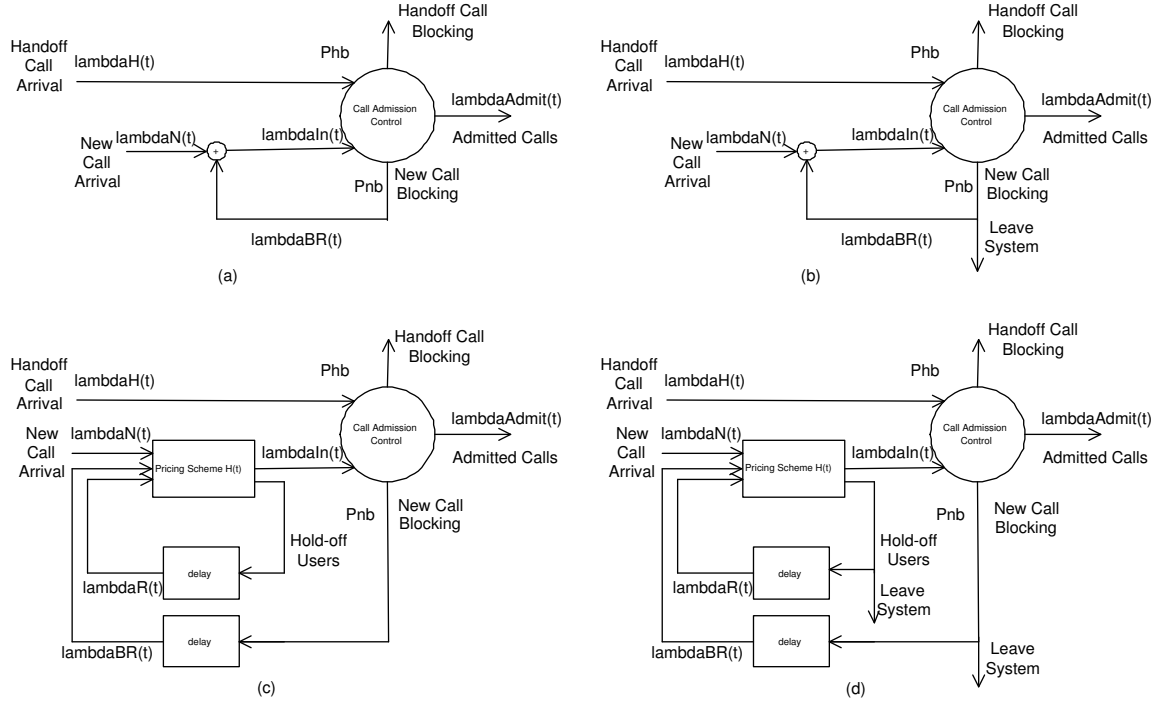


Figure 2.4: Diagrams of experiments CSwR (a), CSwRL (b), PSwR (c) and PSwRL (d)

2.2.4.1 A Dynamic Pricing Scheme for Connection-oriented Services

A dynamic pricing scheme for connection-oriented services in wireless networks based on an analytical approach is presented in [46, 47]. The call duration is modelled as a function of the service price and the user demand is expressed as a decreasing exponential function of the call price per unit time. Furthermore, it is hypothesised that customers tend to prefer transparent, easy to understand pricing policies, and so a linear pricing scheme is imposed. Standard Markovian techniques are used to represent the system evolution and an optimal linear pricing strategy that maximises the network revenue, while providing the required QoS to the users, is described. Performance of the proposed pricing strategy has been compared to the results obtained through a flat-rate charging policy. Simulation results suggest an improvement of 25% in the network revenue and a halving of the blocking probability.

2.2.4.2 Models for 3G/4G Network Pricing

Wallenius and Hamalainen presented models for 3G/4G service pricing including QoS guarantees [48]. Two types of pricing for the different 3GPP [1] traffic classes are introduced. Real-Time connections, such as Conversational and Stream-class traffic, always occupy a whole traffic channel due to the

strict delay requirements of the call, and hence can be charged by the duration and the volume of bits transferred during the call. For non Real-Time Interactive and Background classes, however, a pricing scheme function of the reserved bandwidth is considered more suitable.

Furthermore, it is argued that the full linearity of price to QoS usually produces very low prices for low QoS or very high prices for high QoS guarantees, meaning that the voice call and multimedia call price ratio can be as high as 1:100. To avoid this drawback, a linearity factor is introduced. This is given by:

$$L(x) = A.(e - e^{-B.x})$$

where A and B are linearity parameters and x one of the QoS attributes, either bandwidth, end-to-end delay or bit error rate. The price is then given by:

$$P_b = A_{ij}.(e - e^{-B.x}).T_l$$

where

- P_b is the unit price of the call,
- A_{ij} is a linear price factor for each traffic and subscriber class,
- T_l is the traffic load.

2.3 Dynamic Pricing in Other Industries

2.3.1 General Results on Dynamic Pricing

In [38], Paschadilidis and Liu consider both problems of revenue and welfare maximisation in the context of a loss network with fixed routing. They showed that static pricing is asymptotically optimal in the case of many, relatively small (in terms of network capacity usage) users. This result holds when they incorporate a substitution effect in the demand (people use some alternate network to the one they initially planned to use, because of price). It may be noted that static pricing has some obvious advantages over dynamic pricing: charges may be predicted by users and there is no need for an elaborate real-time price communication system. Furthermore, it is suggested that it may be intractable to compute the optimal (dynamic) policy in a large system, and that recent approximate dynamic programming techniques to compute an approximately optimal policy may be needed.

2.3.2 Fixed Telephony

Some practical pricing experiments have been carried out in students' dormitories [41]. Shih, Katz and Joseph conclude that while time-of-the-day pricing encourages users to shift 30% of their usage from peak to off-peak hours and duration pricing also influences user behaviour; a simple congestion pricing scheme that charges depending on the number of people calling does not influence call duration. It is theorised that users do not change their behaviour because they do not know how long the price increase or decrease will last. Hence it is suggested that, to make a congestion-pricing scheme more effective, the price changes need to be more permanent to entice users to change their behaviour. However, it must be noted that, in this experiments carried out, the price per unit of time varied during the phone call, whereas in most theoretical studies, the price per time unit for a phone call is set at the beginning of the call. Thus the conclusions reached may not be applicable for this study.

2.3.3 Internet and Asynchronous Transfer Mode (ATM)

As explained in [39], at present the Internet relies on technical methods to prevent congestion (the TCP protocol), but includes no mechanism for ensuring QoS guarantees or for delivering service to those users who need it most. Hence congestion and delay have become a characteristic feature of the Internet. Pricing mechanisms have the potential to overcome these shortcomings, resulting in more efficient resource allocation.

There are two possible theoretical approaches to dynamic pricing:

- pricing based on user's bidding for the available bandwidth,
- pricing based on the amount of congestion caused by the users' packets.

The first approach, called "smart market", was developed by MacKie-Mason and Varian [33]: in this case, the network users bid for the available bandwidth and the network serves the highest bidders first. A particular problem with this approach is that it can lead to a backlog of lower bid packets. In addition, the signalling information necessary to complete the bidding may overwhelm the signalling capacity of the cellular networks.

The second approach is based on retrospective "shadow" pricing depending on the amount of congestion caused by the user [26]. This is achieved by marking packets that cause buffers to overflow. In the case of ATM, a particular problem with this approach is that the self-similarity of the traffic makes it difficult to determine when a particular burst of packets ends and when the next one begins

so that marking may be stopped. Also, the fact that this pricing scheme is retrospective means that the user cannot know the price that will be charged in advance.

2.3.4 Other Industries

Real-time (dynamic) pricing has been successfully applied to electricity supplies for both industrial and residential customers [3, 15, 40, 50, 8]. In general, the response of industrial and residential customers to real-time pricing was variable and complex but led to reduced bills for the majority of users.

Another field from which conclusions can be drawn by analogy is financial markets. The prices of shares are governed by the laws of supply and demand and change dynamically over time. Predictions for the behaviour of telecommunication networks with dynamic pricing can be made by analogy with the behaviour of the financial markets. In both cases, the choices that consumers make are dependent on price as well as additional (chaotic or random) factors.

In the case of revenue maximisation, the problem is essentially a problem of *yield management*, similar to the problems that arise in the airline and other service industries [43, 42]. The common problem in this case is that the marginal cost of serving an additional customer, e.g. an airline passenger or a new call, is negligible once a flight has been scheduled or a communication infrastructure is in place [39]. However in cellular network the problem is technically slightly different: the operator considers a long-term average whereas in airline industry a finite horizon is set (the departure of the plane) [38].

2.4 Conclusions

For establishing the network pricing policy, two fundamentally opposed approaches can be used as described in section 2.2.1, but the most realistic and interesting approach is to find a trade-off between the network utilisation and the provider revenue.

The most complete, and detailed, study of dynamic pricing in cellular networks has been carried out by Hou, Yang and Papavassiliou (c.f. section 2.2.3). In this work, it was established that there exists an optimal constant arrival rate to the system for optimising the total user utility, and a pricing scheme was designed to make the arrival traffic rate fit the optimal one. The optimal arrival rate was calculated for a steady state, whereas in the real system the regulation of the demand by the price cannot be perfect. Hence, as the arrival of traffic into the pricing scheme will vary during the day, the arrival rate into the system will vary also. For this reason, the optimal arrival rate for the

real system may be different than the optimal arrival rate for the steady state, as some variation around it must be taken into account. Because regulation of the traffic by the pricing scheme is not immediate, signalling that the network is congested before this actually occurs could improve the total utility of the users by limiting the number of blocked calls. The operator revenue could also be increased if peak-prices start being charged before the network is congested. On the other hand, starting to charge peak-prices too early might lead to a reduction of profit due to a decrease in the number of users in the network.

For these reasons, it seems particularly interesting to make the “optimal” value used in this pricing scheme vary from the steady state result and to see how the total utility and revenue over a day is affected. This is one of the main goals of this work. In the following chapter, an analytic study of the the total utility and the revenue over a day is performed.

Chapter 3

Network Modelling

This chapter presents the models used to represent the network and to generate network traffic. Two types of traffic are generated: GSM and GPRS traffic. The models used for these are now described in details.

3.1 Traffic Model

3.1.1 GSM Traffic Model

A Poisson process is used to generate the arrival of GSM calls. The call arrival rate varies depending on the time of the day (see Figure 3.1). The GSM call holding time (total call duration) and cell dwell time (time a mobile host stays in a cell) are modelled using a geometrical distribution. They are assumed to be independent of both price and time. When a call is generated, both its call holding time and cell dwell time are generated and the minimum of these two is used to determine a suitable event trigger to associate with the call.

3.1.2 GPRS Traffic Model

GPRS traffic is generated according to the IETF web traffic model proposed in [22]. It is a unidirectional model: it represents the packets from a source, which may be at either end of the link, and ignores the uplink traffic. According to this model a web browsing *session* consists of *packet calls* (see Figure 3.2). Each time a user requires an information entity, a packet call is generated. A packet call is composed of a certain number of *packets*, hence it constitutes a bursty sequence of packets, a characteristic of packet transmission in a fixed network.

A packet service session contains one or several packet calls depending on the application. For example in a web browsing session, a packet call corresponds to the downloading of a web document. After the document has been successfully downloaded to the terminal, the user takes a certain amount of time to study the information it contains. This time interval is called the *reading time*. It is also possible that the session contains only one packet call; for example for a file transfer, in this case the session includes no reading time.

The model is made of the following components:

Session Arrival Process: The session arrival in the system is modelled as a Poisson process.

Number of packets calls request by session: This is a geometrically distributed random variable with a mean of 5 packets per session.

Reading time between packet calls: The reading time between two consecutive packet call requests in a session is a geometrically distributed random variable with a mean of 412 seconds. The reading time starts when the last packet of the packet call is completely received by the user. It ends when the user makes a request for the next packet call.

Number of packets in a packet call: According to the IETF traffic model, this parameter should vary depending on the characteristics of UMTS traffic. It is suggested that a geometrically distributed random variable with a mean of 25 packets is suitable, and this is used in this simulator.

Time interval between packets: The time interval between two consecutive packets inside a packet call is a geometrically distributed random variable with a mean which depends of the average bit rate at the source level. The traffic generator implemented simulates a source with an average bit rate of 64 kb/s; in this case the mean value of the time interval between two consecutive packets in a packet call is 62.5 ms.

Packet size: The packet size is modelled using a Pareto distribution with cut-off.

The Pareto distribution (without cut-off) is defined by:

$$\begin{aligned}
 f_x(x) &= \frac{\alpha \cdot k^\alpha}{x^{\alpha+1}}, x \geq k \\
 F(x) &= 1 - \left(\frac{k}{x}\right)^\alpha, x \geq k \\
 \mu &= \frac{k\alpha}{\alpha - 1}, \alpha > 1 \\
 \sigma^2 &= \frac{k^2 \cdot \alpha}{(\alpha - 2)(\alpha - 1)}, \alpha > 2
 \end{aligned}$$

A cut-off of $m= 66666$ bytes is used and the packet size is defined by :

$$PacketSize = \min(P, m)$$

where P is a normal Pareto distributed random variable with parameters $\alpha = 1.1$ and $k = 81.5$ bytes.

A summary of the GPRS model and the parameters used is given in Table 3.1.

Parameter	Distribution
session arrival process	Poisson
number of packet call requests	Geom(5)
reading time	Geom(412 s)
number of packets in a packet call	Geom(25)
time interval between consecutive packets	Geom(62.5 ms)
packet size	$\min(\text{Pareto}(\alpha = 1.1, k = 81.5b), 66666)$,

Table 3.1: Summary of GPRS model

3.2 Call Admission Control

As discussed in section 2.1, many different schemes for call admission control have been proposed, but as yet, none of these has been accepted as a standard. One of the most common schemes, the Guard Channel Scheme is used in this study. In this scheme a number, C_h , of guard channels taken from the total number of channels, C , are reserved for exclusive use by hand-off calls, but specific channels are not reserved. That is, a new call will be accepted if the total number of calls already in progress is less than $C - C_h$, while a hand-off call will be served unless all C channels are occupied.

3.3 Network Topology

Mobile networks are made up of cells, which are geographic areas which depends on a specific base station. The main characteristic feature of wireless networks is the mobility of the users, hence cells are interdependent as part of the traffic in one cell can migrate to the neighbouring cells. Thus to simulate mobile networks, this interaction (or traffic mobility) has to be taken into account. While in reality cells have chaotic shapes, a conventional way of modelling them is to use a hexagonal representation. The traffic coming from neighbouring cells (hand-off traffic) is either modelled or generated by the simulation of these neighbouring cells.

3.3.1 Hand-off Call Modelling

The hand-off traffic arriving in a cell depends of the current traffic in neighbouring cells, on the mobility of users and on the hand-off blocking probability. In [32], the following hand-off traffic model is defined:

$$\lambda_h = \frac{\eta \cdot (1 - p_{nb})}{\mu + \eta \cdot P_{hb}} \lambda_{in} \quad (3.1)$$

where

- λ_h is the hand-off call arrival rate,
- λ_{in} is the new call arrival rate in the admission block,
- P_{nb} the new call blocking probability in the admission block,
- P_{hb} the hand-off call blocking probability in the admission block,
- $1/\eta$ the mean cell dwell time,
- $1/\mu$ the mean call holding time.

3.3.2 Hand-off Call Generation

The second solution is to run the simulation using several cells. However, the border of the network is still a problem as it can influence traffic in the centre cells. In [37], Orlik and Rappaport present and compare several models for hand-off calls, including some with the simulation of a cluster of cells instead of a single one. They solved analytically the case of a network whose coverage region consists of seven cells in isolation. The results for different models are compared with this solution and it is concluded that the single isolated cell which use a Poisson distribution to model hand-off calls arrival has similar results to other models while requiring less states. However their models using cell clusters model hand-off calls at the border of the system, so the traffic generated at the centre of the system may not be really accurate. Furthermore, to study pricing, as the price of a call is set as the call enters the system, a price needs to be generated for hand-off calls, as the current price may not be accurate.

In [18], a solution is proposed to eliminate the border effect by wrapping cells around like on a football, as show in figure 3.3. This enables the generation of hand-off calls and so alleviates the problem of setting a price for them and, if the network size is big enough, should remove the border effect and hence be a good model of a broad network. This model will be used for some simulations experiments (see section 6.4).

3.4 Conclusion

In this chapter, a model for cellular networks has been presented, alongside with a traffic model. In the following chapter, a mathematical analysis is carried out on a simplified version of this model.

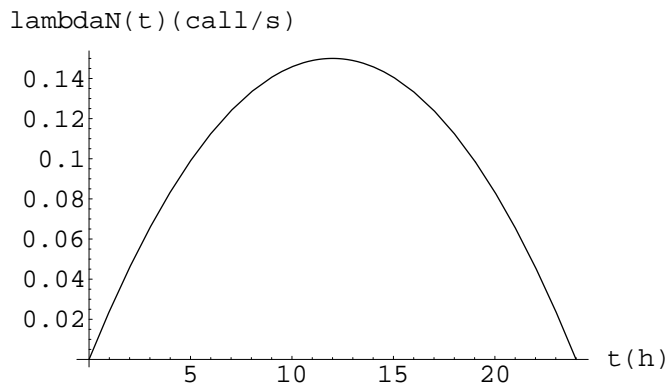


Figure 3.1: Arrival rate variation during the day

instants of packets arrivals to
base station buffer

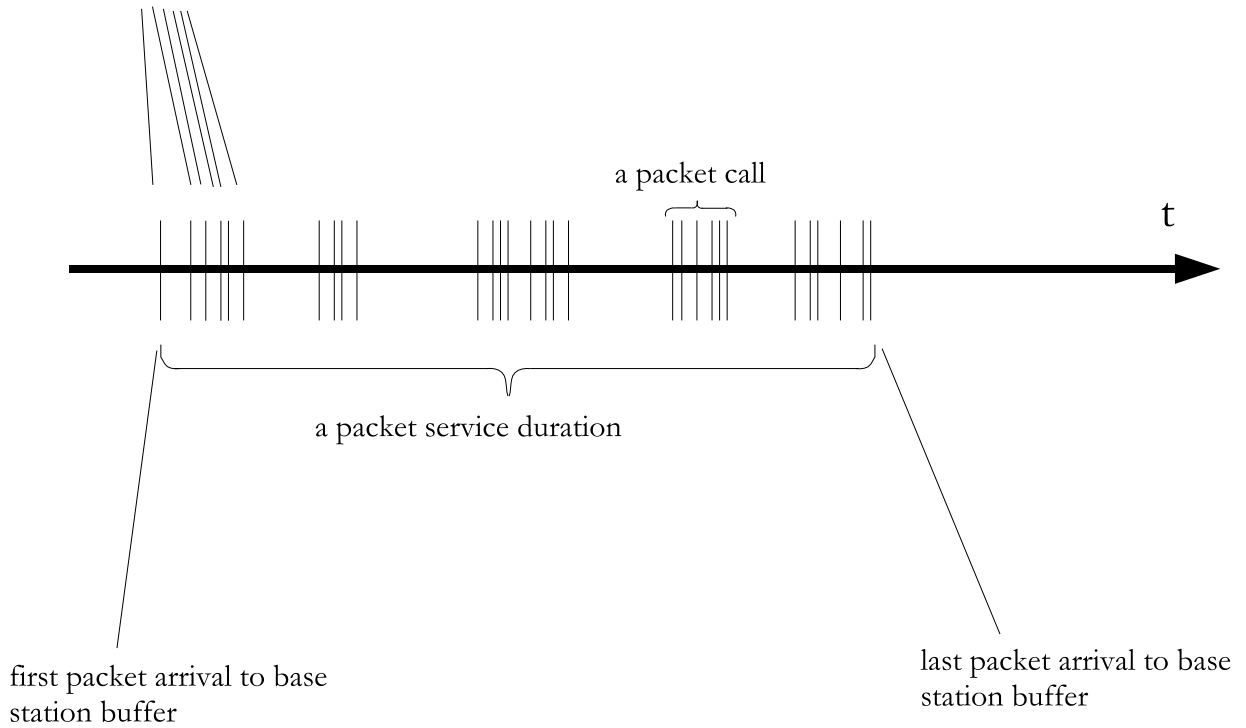


Figure 3.2: Model of a packet service session

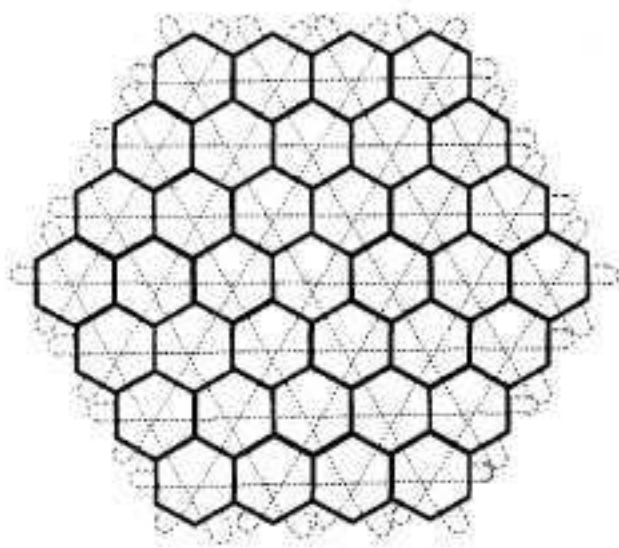


Figure 3.3: Wrap-around network topology

Chapter 4

Mathematical Analysis

The goal of this chapter is to present a basic mathematical analysis of the pricing scheme for cellular networks proposed by Hou, Yang and Papavassiliou [21]. This model will provide a theoretical basis for getting a detailed understanding of the behaviour of the pricing scheme and a comparison model for use with experimental results. The first section presents the model used for this analysis; an analytic expression for the traffic admitted in the system is then established. In section 4.3, the revenue function is studied and the chapter concludes with an analysis of the total utility. This work was carried out with Mustapha Bouhtou of *France Telecom Research and Development*.

4.1 Model

A mobile network is a complex system and it may not be possible to produce a tractable model of such a system. In this analysis a number of simplifications are made to produce a model that captures the essential behaviour of the system. The main assumption made is to ignore all hand-off calls. This is a significant simplification as hand-off calls make up approximately two thirds of the traffic in the model used [21]. However, there is no universally agreed hand-off call model (c.f. section 3.3.1), and as the hand-off call rate depends on several parameters (new call entrance rate, hand-off call probability, cell dwell time, call duration), including hand-off calls makes the model significantly more complex.

It will also be assumed that all users quit the system if they find the price too high or if their call is blocked.

4.2 Traffic Admitted in the System

The same call variational arrival rate model as described in [21] will be used. In this model, the traffic generation rate follows a parabolic function $\lambda_n(t)$ during the day, as in figure 4.1. However,

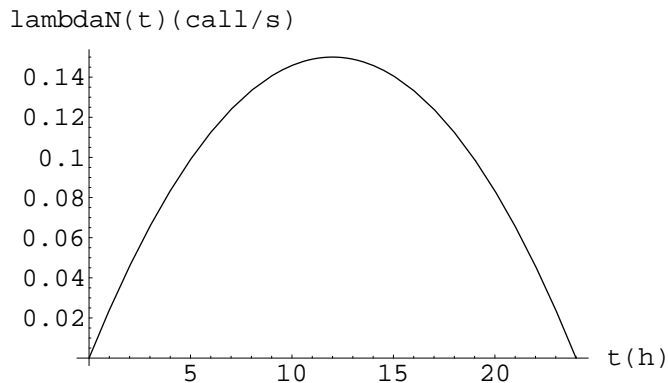


Figure 4.1: $\lambda_n(t)$, The new call arrival function

the specific shape of the new call arrival rate function does not play any part in this analysis; it is only used to obtain a graphical understanding of the problem. Assuming that the pricing scheme chosen regulates the traffic perfectly, the traffic entering the system is:

$$\lambda_{in}(t) = \min(\lambda_n(t), \lambda_n^*) \quad (4.1)$$

where λ_n^* is the target rate, i.e. the rate the pricing scheme aims to produce at the entrance of the system.

If we assume that all calls are of equal length, τ , the maximum admission rate to the system in steady state is $\lambda_{cap} = C/\tau$ where C is the network capacity. As the arrival rate varies slowly in comparison to the life-time of a call τ , we will model the state of the system as a succession of steady states. Under this assumption, the call admission control block will accept calls at a rate $\lambda_{admit}(t) = \min(\lambda_{in}(t), \lambda_{cap})$. The complete expression for the admission rate in the system is:

$$\lambda_{admit}(t) = \min(\lambda_n(t), \lambda_n^*, \lambda_{cap}) \quad (4.2)$$

Figure 4.2 shows the variation of $\lambda_{admit}(t)$ over time. The maximal value corresponds to $\min(\lambda_n^*, \lambda_{cap})$.

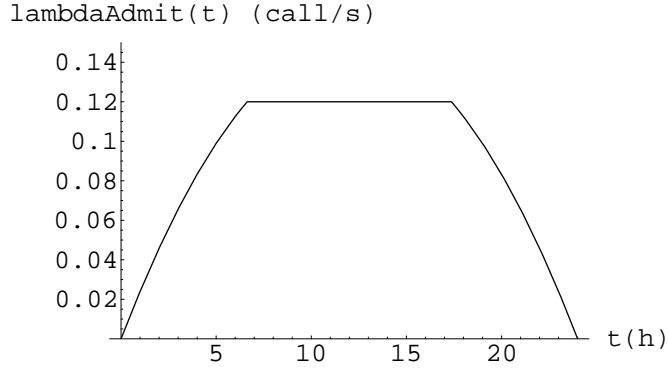


Figure 4.2: $\lambda_{admit}(t)$, The call admission rate

4.3 Revenue

The variation of the network operator revenue as a function of λ_n^* is considered. To do this, the pricing scheme must be defined.

4.3.1 Price

The pricing scheme defined in [21] by Hou, Yang and Papavassiliou is used:

$$p(t) = \begin{cases} p_0 & \text{when } \lambda_n(t) \leq \lambda_n^* \\ p_0 \left(1 + \sqrt{\ln \left(\frac{\lambda_n(t)}{\lambda_n^*} \right)} \right) & \text{when } \lambda_n(t) \geq \lambda_n^* \end{cases}$$

The variation of this pricing scheme as a function of λ_n and as a function of the time of the day with an arrival rate $\lambda_n(t)$ as defined in the previous section, are shown in figures 4.3 and 4.4 respectively.

4.3.2 Revenue

The expression for the revenue depends of the relative values of λ_n^* and λ_{cap} ; we will consider both cases:

- For $\lambda_n^* < \lambda_{cap}$, the network is never actually congested, hence $\lambda_{admit}(t) = \min(\lambda_n(t), \lambda_n^*)$. In

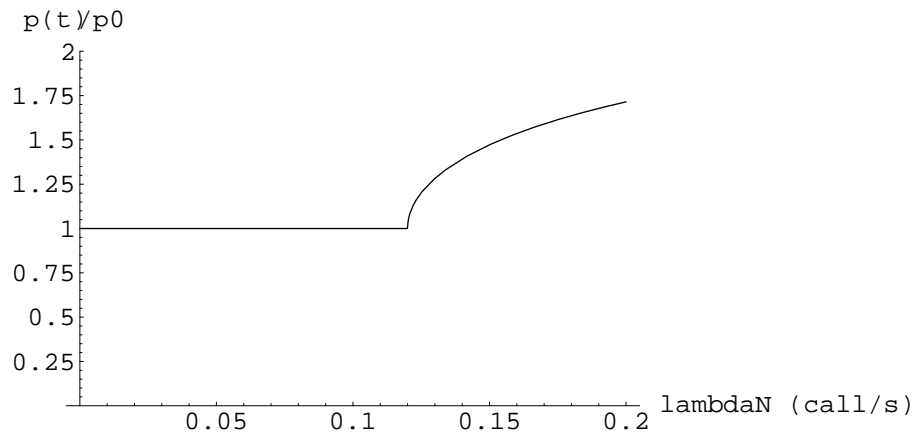


Figure 4.3: Price variation with λ_n

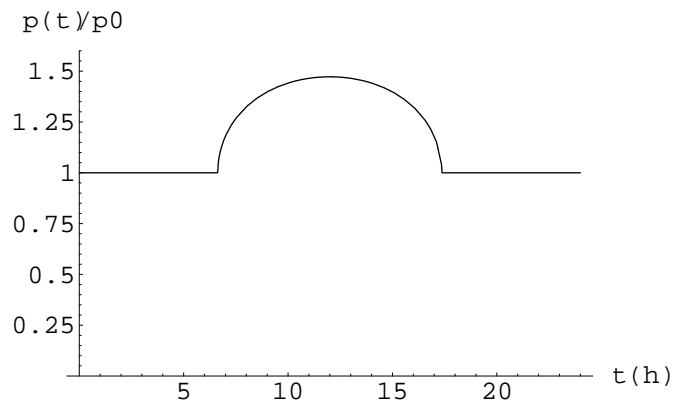


Figure 4.4: Price variation with time for an arrival rate $\lambda_n(t)$

this case the revenue per unit of time dt is

$$dR(\lambda_n^*) = \begin{cases} \tau \cdot p_0 \cdot \lambda_n(t) \cdot dt & \text{when } \lambda_n(t) \leq \lambda_n^* \\ \tau \cdot p_0 \left(1 + \sqrt{\ln \left(\frac{\lambda_n(t)}{\lambda_n^*} \right)} \right) \cdot \lambda_n^* dt & \text{when } \lambda_n(t) \geq \lambda_n^* \end{cases}$$

Hence, $R(\lambda_n^*) = R_1(\lambda_n^*) + R_2(\lambda_n^*)$ where

$$R_1(\lambda_n^*) = \tau \cdot p_0 \int_{\lambda_n(t) \leq \lambda_n^*} \lambda_n(t) \cdot dt$$

$$R_2(\lambda_n^*) = \tau \cdot p_0 \cdot \lambda_n^* \int_{\lambda_n(t) > \lambda_n^*} \tau \left(1 + \sqrt{\ln \left(\frac{\lambda_n(t)}{\lambda_n^*} \right)} \right) dt$$

- For $\lambda_n^* > \lambda_{cap}$, the entrance rate to the CAC block is limited by the system capacity rather than the pricing scheme, hence $\lambda_{admit}(t) = \min(\lambda_n(t), \lambda_{cap})$. In this case, the revenue per unit of time dt is

$$dR(\lambda_n^*) = \begin{cases} \tau \cdot p_0 \cdot \lambda_n(t) \cdot dt & \text{when } \lambda_n(t) \leq \lambda_{cap} \\ \tau \cdot p_0 \cdot \lambda_{cap} \cdot dt & \text{when } \lambda_{cap} < \lambda_n(t) < \lambda_n^* \\ \tau \cdot p_0 \cdot \lambda_{cap} \cdot \left(1 + \sqrt{\ln \left(\frac{\lambda_n(t)}{\lambda_n^*} \right)} \right) dt & \text{when } \lambda_n^* < \lambda_n(t) \end{cases}$$

Hence, $R(\lambda_n^*) = R_3(\lambda_n^*) + R_4(\lambda_n^*) + R_5(\lambda_n^*)$ where

$$R_3(\lambda_n^*) = \tau \cdot p_0 \cdot \int_{\lambda_n(t) \leq \lambda_{cap}} \lambda_n(t) \cdot dt$$

$$R_4(\lambda_n^*) = \tau \cdot p_0 \cdot \lambda_{cap} \cdot \int_{\lambda_{cap} < \lambda_n(t) < \lambda_n^*} dt$$

$$R_5(\lambda_n^*) = \tau \cdot p_0 \cdot \lambda_{cap} \cdot \int_{\lambda_n(t) > \lambda_n^*} \left(1 + \sqrt{\ln \left(\frac{\lambda_n(t)}{\lambda_n^*} \right)} \right) dt$$

The resulting expression for the revenue is:

$$R(\lambda_n^*) = \tau \cdot p_0 \cdot \int_{\lambda_n(t) \leq \min(\lambda_n^*, \lambda_{cap})} \lambda_n(t) \cdot dt + \tau \cdot p_0 \cdot \min(\lambda_n^*, \lambda_{cap}) \cdot \int_{\lambda_n(t) > \min(\lambda_n^*, \lambda_{cap})} \left(1 + \sqrt{\ln \left(\max \left(\frac{\lambda_n(t)}{\lambda_n^*}, 1 \right) \right)} \right) dt$$

Mathematica 4.2 has been used to study the variation of $R(\lambda_n^*)$. It was not possible to obtain an analytical expression of the derivative of the revenue, therefore the variation of the revenue was studied qualitatively. As λ_n^* increases from zero, it can be seen qualitatively that the revenue will initially increase as calls enter the network (for $\lambda_n^* = 0$, no traffic enters the system). The variation of the revenue is unknown until $\lambda_n^* = \lambda_{cap}$.

For $\lambda_{cap} < \lambda_n^* < \lambda_{max}$, $R(\lambda_n^*) = R_3(\lambda_n^*) + R_4(\lambda_n^*) + R_5(\lambda_n^*)$ where $R_3(\lambda_n^*)$ is independent of λ_n^* , and the sum $R_4(\lambda_n^*) + R_5(\lambda_n^*)$ is a decreasing function of λ_n^* (it is a constant traffic share, which is priced at the off-peak price when the rate is below λ_n^* and at the peak price (which is decreasing with λ_n^*) otherwise). Hence $R(\lambda_n^*)$ is decreasing for $\lambda_{cap} < \lambda_n^* < \lambda_{max}$.

For $\lambda_{max} < \lambda_n^*$, $R(\lambda_n^*) = R_3(\lambda_n^*) + R_4(\lambda_n^*) + R_5(\lambda_n^*)$ where $R_3(\lambda_n^*)$ is independent of λ_n^* , $R_4(\lambda_n^*)$ is a constant and $R_5(\lambda_n^*)$ is zero, hence $R(\lambda_n^*)$ is constant.

This analysis may be validated by considering figure 4.5 (plotted using *Mathematica 4.2*). The value of λ_n^* which optimises the network revenue is approximately $\lambda_n^* = 0.11$ call/second.

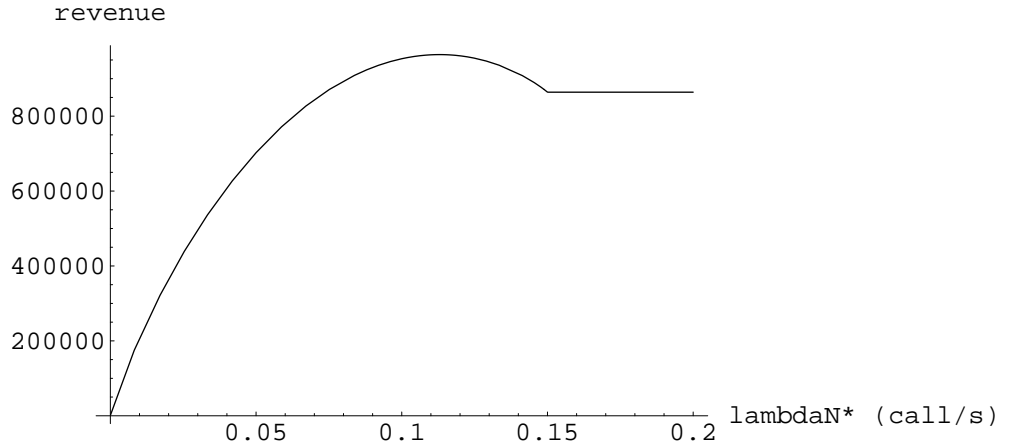


Figure 4.5: Revenue variations

4.4 Utility

In this section, we will establish an expression for the total utility over a day. First, an expression for the blocking probability is found and a model of the utility of a single user is presented. Finally, a formula for the total utility is established.

4.4.1 Blocking Probability

Assuming that the call arrival rate is exactly $\lambda_n(t)$ and that the duration of each call is equal to the average call duration τ , the probability that a call is blocked is zero when the arrival rate is below the maximal arrival rate in steady state λ_{cap} ; hence:

$$P_b(t) = \begin{cases} 0 & \text{when } \lambda_n(t) < \lambda_{cap} \\ \frac{\lambda_{in}(t) - \lambda_{admit}(t)}{\lambda_{in}(t)} & \text{when } \lambda_n(t) > \lambda_{cap} \end{cases}$$

As $\lambda_{in}(t) = \min(\lambda_n(t), \lambda_n^*)$ and $\lambda_{admit}(t) = \min(\lambda_n(t), \lambda_n^*, \lambda_{cap})$ (c.f. equations 4.1 and 4.2),

$$P_b(t) = \begin{cases} 0 & \text{when } \lambda_n(t) < \lambda_{cap} \\ 1 - \frac{\min(\lambda_n^*, \lambda_{cap})}{\min(\lambda_n(t), \lambda_n^*)} & \text{when } \lambda_n(t) > \lambda_{cap} \end{cases}$$

Figure 4.6 shows the variations of the blocking probability during the course of one day, when the arrival traffic rate is $\lambda_n(t)$.

4.4.2 Utility of a Single User

The utility function presented in [28] and used by Hou, Yang and Papavassiliou [21] is used to model the utility of a single user:

$$U(P_b) = \begin{cases} 1 - e^{30(P_b - 10 \cdot P_L)} & \text{when } 0 \leq P_b \leq P_L \\ 0 & \text{when } P_b > P_L \end{cases}$$

P_L is set at 0.01, as in [21]. Figure 4.7 shows the variation of this utility function with blocking probability P_b . This model assumes that the utility of users hardly degrades as the blocking probability

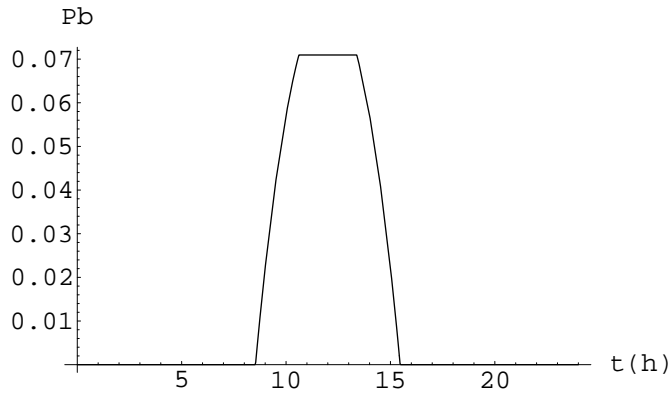


Figure 4.6: Variation of the blocking probability over one day

increases up to a certain limit probability P_L . However, after this limit, the utility drops suddenly: users will not accept the service when the QoS is worse than a pre-specified threshold.

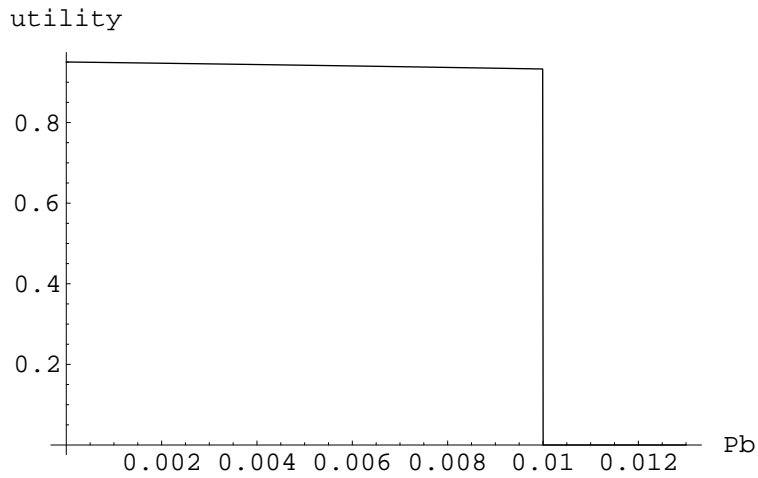


Figure 4.7: Variation in the utility of a single user with the blocking probability

If we call λ_L the arrival rate so that $P(\lambda_L) = P_L$, then $\lambda_{cap} < \lambda_L$ and the utility can be expressed as:

$$U(t) = \begin{cases} U_0 \text{ where } U_0 = 1 - e^{-300 \cdot P_L} & \text{when } \lambda_n(t) < \lambda_{cap} \\ 1 - e^{30 \left(1 - \frac{\min(\lambda_n^*, \lambda_{cap})}{\min(\lambda_n(t), \lambda_n^*)} - 10 \cdot P_L \right)} & \text{when } \lambda_{cap} \leq \lambda_n(t) \leq \lambda_L \\ 0 & \text{when } \lambda_n(t) \geq \lambda_L \end{cases}$$

4.4.3 Total Utility

4.4.3.1 Expression

The expression for the utility varies with the value of λ_n^* as it is compared to λ_{cap} and λ_L . The three cases are now studied in detail:

- If $\lambda_n^* < \lambda_{cap}$, then the pricing strategy will block any increase in the arrival rate before the system is congested, hence the blocking probability is always zero and the utility of a single user is constant, equal to U_0 . In this case the expression of the total utility is:

$$U_{T1}(\lambda_n^*) = U_0 \cdot \left[\int_{\lambda_n(t) < \lambda_n^*} \lambda_n(t) \cdot dt + \lambda_n^* \cdot \int_{\lambda_n(t) > \lambda_n^*} dt \right]$$

- If $\lambda_{cap} < \lambda_n^* < \lambda_L$, then the system will be congested during some periods of the day, but the blocking probability will never reach P_L and the utility of a single user will never be zero. In this case, the expression for the blocking probability is:

$$P_b(t) = \begin{cases} 0 & \text{when } \lambda_n(t) < \lambda_{cap} \\ 1 - \frac{\lambda_{cap}}{\lambda_n(t)} & \text{when } \lambda_{cap} < \lambda_n(t) < \lambda_n^* \\ 1 - \frac{\lambda_{cap}}{\lambda_n^*} & \text{when } \lambda_n(t) > \lambda_n^* \end{cases}$$

The expression for the utility in this case is:

$$\begin{aligned} U_{T2}(\lambda_n^*) &= U_0 \cdot \int_{\lambda_n(t) < \lambda_{cap}} \lambda_n(t) \cdot dt + \lambda_{cap} \cdot \int_{\lambda_{cap} < \lambda_n(t) < \lambda_n^*} 1 - e^{30 \left(1 - 10 \cdot P_L - \frac{\lambda_{cap}}{\lambda_n(t)} \right)} dt \\ &\quad + \lambda_{cap} \cdot \left(1 - e^{30 \left(1 - 10 \cdot P_L - \frac{\lambda_{cap}}{\lambda_n^*} \right)} \right) \int_{\lambda_n(t) > \lambda_n^*} dt \end{aligned}$$

- If $\lambda_L < \lambda_n^*$, then for $\lambda_L < \lambda_n(t)$, the blocking probability exceeds P_L , hence the utility is zero, so the total utility is independent of λ_n^* . In this case the expression for the utility is:

$$U_{T3}(\lambda_n^*) = U_0 \cdot \int_{\lambda_n(t) < \lambda_{cap}} \lambda_n(t) \cdot dt + \lambda_{cap} \cdot \int_{\lambda_{cap} < \lambda_n(t) < \lambda_L} 1 - e^{30 \left(1 - 10 \cdot P_L - \frac{\lambda_{cap}}{\lambda_n(t)} \right)} dt$$

The complete expression of the total utility is, therefore:

$$U_T(\lambda_n^*) = \begin{cases} U_0 \cdot \left[\int_{\lambda_n(t) < \lambda_n^*} \lambda_n(t) \cdot dt + \lambda_n^* \cdot \int_{\lambda_n(t) > \lambda_n^*} dt \right] & \text{when } \lambda_n^* < \lambda_{cap} \\ U_0 \cdot \int_{\lambda_n(t) < \lambda_{cap}} \lambda_n(t) \cdot dt + \lambda_{cap} \cdot \int_{\lambda_{cap} < \lambda_n(t) < \lambda_n^*} 1 - e^{30 \left(1 - 10 \cdot P_L - \frac{\lambda_{cap}}{\lambda_n(t)} \right)} dt \\ \quad + \lambda_{cap} \cdot \left(1 - e^{30 \left(1 - 10 \cdot P_L - \frac{\lambda_{cap}}{\lambda_n^*} \right)} \right) \cdot \int_{\lambda_n(t) > \lambda_n^*} dt & \text{when } \lambda_{cap} < \lambda_n^* < \lambda_L \\ U_0 \cdot \int_{\lambda_n(t) < \lambda_{cap}} \lambda_n(t) \cdot dt + \lambda_{cap} \cdot \int_{\lambda_{cap} < \lambda_n(t) < \lambda_L} 1 - e^{30 \left(1 - 10 \cdot P_L - \frac{\lambda_{cap}}{\lambda_n(t)} \right)} dt & \text{when } \lambda_L < \lambda_n^* \end{cases}$$

4.4.3.2 Variation

$U_{T1}(\lambda_n^*)$ increases with λ_n^* (as the product of a constant and an increasing function of λ_n^*). The variation of $U_{T2}(\lambda_n^*)$ is less obvious; consider its derivative:

$$U'_{T2}(\lambda_n^*) = -\lambda_{cap} \cdot e^{30 \left(1 - 10 \cdot P_L - \frac{\lambda_{cap}}{\lambda_n^*} \right)} \int_{\lambda_n(t) > \lambda_n^*} dt$$

This derivative is negative, hence $U_{T2}(\lambda_n^*)$ decreases with λ_n^* . $U_{T3}(\lambda_n^*)$ is independent of λ_n^* . The value of the total utility is, hence, a maximum for $\lambda_n^* = \lambda_{cap}$, that is when the system is said to be congested and actually is. This is quite plausible because with the model used for this mathematical analysis, this is the value at which the total number of users will be maximised, while the blocking probability remains zero. This analysis can be validated graphically, see figure 4.8 (plotted by *Mathematica 4.2*).

4.5 Conclusions and Limitation of the Mathematical Analysis

In this chapter a mathematical analysis of a simplified model has been studied. Analytical expressions for both the aggregated revenue and the utility over a whole day have been established and their variation studied. The values of the target new call arrival rate λ_n^* that optimise the network operator

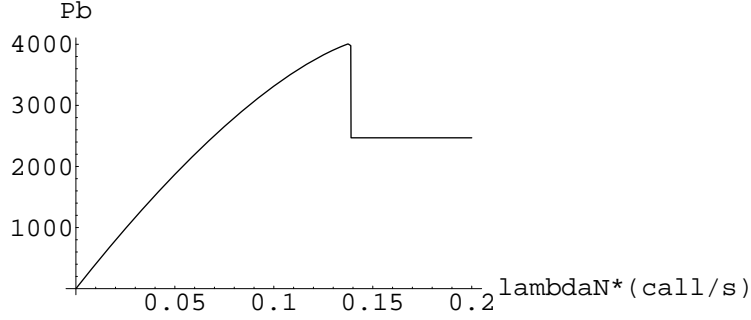


Figure 4.8: Variations in total utility

revenue and the total utility of users differ significantly (0.11 and 0.1375 respectively). Therefore, a trade-off has to be found between maximising the network operator revenue and the total utility of users.

This analysis suggests that there are optimal values for the target new call arrival rate that maximises the network operator revenue and the total utility and that these may differ. However, the simplifications and assumptions used to make this model tractable mean that it might not represent the network completely. We review each of the assumptions made and examine their potential impact on the results above.

This model does not include hand-off calls. This should mainly influence the blocking probability, as in the real scheme this is a weighted average of the hand-off and new call blocking probability (these are different due to the CAC scheme used).

It is also assumed that the regulation by the price is perfect; this will lead to a reduction in the blocking probability when compared with the modelled system. This effect will be increased by the simplification used to model the system as a succession of steady states. The assumption that all calls last for the same length of time smoothes the variations of the blocking probability and, hence, the price. The fact that the arrival of the calls is assumed to be an arrival of rate exactly $\lambda_n(t)$ and not a Poisson process of mean $\lambda_n(t)$ will augment this effect. When considering the revenue, these variations should be averaged, whereas for the total utility, because of the preset threshold value, the result may differ significantly.

Finally, the assumption that all hold-off or blocked users leave the system could lead to a reduced blocking probability, hence an increased utility and a reduced revenue in comparison to the real

system.

For these reasons, the validity of the above mathematical model may be questionable. The main concern relates to the blocking probability, which influences in particular the total utility. In the following chapters, the simulator implemented, the model designed and the results obtained by simulations are described and analysed.

Chapter 5

Simulator Description

Having examined existing network models and analysed a simple analytical model, the motivations for using and writing a simulator are now presented together with the specification and design of the simulator written. Some detail relating to its technical features are given and the chapter concludes with a description of the process used to validate the simulator.

5.1 Motivations

5.1.1 Motivations for Using a Simulator

Cellular networks are complex systems, not only due to their structure but also due to the complexity of their traffic. A cellular network covers a broad geographical area which is divided into cells. Users may migrate between cells while making or receiving phone calls. When a request to start or continue a call in a cell is made, the network has to decide if it will assign the necessary resources to this call or reject it. This will depend on the current traffic in the system. The traffic generated in cells may vary both temporally and spatially. The mobility of users makes the specification of the total traffic in the network even more complex. This complexity is hard to model mathematically: treated in isolation each element may be successfully modelled, but their combination cannot be, especially when considering a large number of cells. Whereas an approximate analytical formulation and its solution can be useful for designing algorithms and getting a detailed understanding of how they influence the traffic, their evaluation requires testing with more accurate models. It is particularly difficult to run practical experiments of such scope, hence the use of simulation provides a useful solution: the system may be modelled in great detail while still providing a suitable environment for testing algorithms.

5.1.2 Motivations for Writing a new Simulator

Simulation is used in a wide variety of research domains and a large number of simulators are available for use. Whereas several simulators of computer networks exist, the number of simulators for cellular networks is much smaller. The simulator required for this work needs to handle call generation, call admission, resource management and mobility of users in a cellular network.

Some of the big multi-purpose simulators include a GSM/GPRS module. For example, a GPRS module [23] for the widely used simulator NS2 [4] is available. However this module aims to model low level communication (packet level) and does not provide higher functionality such as resource management or call hand-off. While extending the simulator to provide these functionalities is possible, the fact that the simulator handles so many low level details makes it exceedingly slow to obtain meaningful results when using it for the purpose of this study. Furthermore, as this module has not been designed to handle several cells, extending it to provide this functionality could prove problematic. The commercial simulator OPNET also includes a GPRS module, but it also does not support hand-off between cells.

The lack of an adequate simulator meant it was either necessary to extend an existing one or write one from scratch. The low-level nature of existing simulators means it is very slow to compute many higher level operations, so the decision to write a new simulator was made.

5.2 Specifications

The focus of this work is on pricing in cellular networks, and any simulator written must include the following features:

- cellular network traffic generation,
- call admission,
- resource management,
- call mobility,
- pricing.

The simulator should be able to model several cells over several days, with a time- and space-dependent traffic generation rate . It should also be possible to measure several performance metrics such as the variation of traffic, price and revenue over a variety of time periods.

5.3 Design

5.3.1 Level of Abstraction

For a simulation model to be accurate and efficient, the correct level of detail required needs to be determined as a function of both the specific issues to be investigated and the evaluation methodology used. As for this work focuses on resource management, the level of abstraction chosen is the individual call: to evaluate the resource management at the channel level, it is not necessary to know the number of packets sent, as a channel is reserved for each call during its entire duration.

5.3.2 Different Simulator Types

A simulator can either model events discretely or using a continuous, fluid model. In the first case, each event is simulated, while in the second case the global behaviour of several events is considered. The first method is the closest to real network behaviour, however the second method may be more efficient for modelling a large number of events.

The simulator can be either event-driven or time driven. An event-driven simulator is continuous: each event is processed one after the other, with the simulation clock advancing from one event time to the next. In a time driven simulator, time is split into small intervals, and the simulator clock advances by fixed increments; hence the simulation is discrete. At the end of each time interval, the state of the system is updated with the results of all the events that are scheduled during the interval. Event-driven simulation can produce results with a great level of precision; on the other hand time-driven simulator can be easily implemented on a parallel architecture, hence reducing the execution time.

The number of calls per cell per day is bounded by the cell capacity and the call level abstraction makes it feasible to simulate each call. Hence, for this work, it has been chosen to write a discrete event, event-driven simulator .

5.3.3 Different Types of Events

In this simulator, the different events are the start or end of a phone call or GPRS session. The four different events types occurring during the simulation are *EventStartGSM* and *EventStartGPRS* that model the beginning of a GSM call and a GPRS session respectively and *EventCloseGSM* and *EventCloseGPRS* which model the corresponding end of calls or session. Figure 5.1 shows the hierarchy of the different type of events.

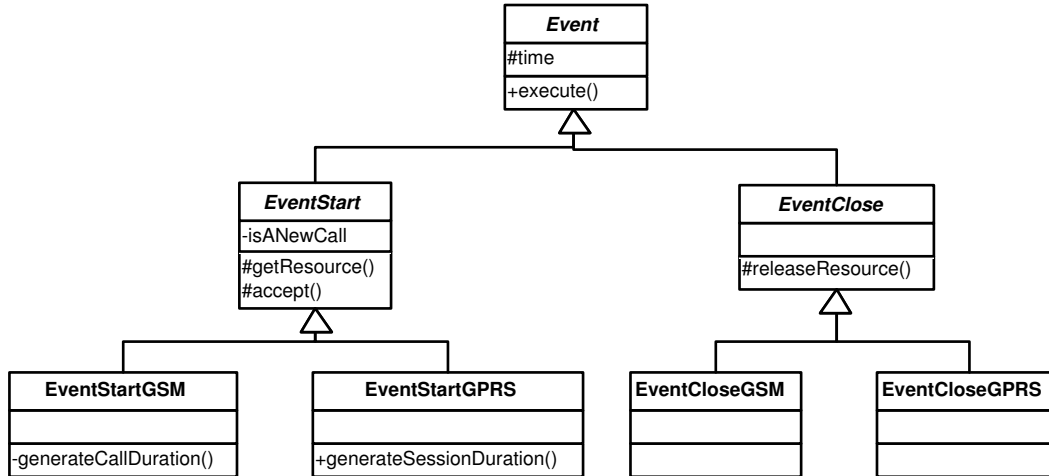


Figure 5.1: Events hierarchy

During the initialisation of the simulator, an event of each type is generated. All events are stored in an *EventList*, ordered by their time of execution. The first event is executed. During this execution an event of the same type plus possibly a related event may be created and scheduled. This is repeated until the execution time of the next (i.e. first in the list) event exceeds the total time simulated. During the execution of an *EventStart*, the following *EventStart* of the same type is created, as well as the corresponding *EventClose*. During the execution of an *EventClose* an *EventStart* of the same type may be generated if the network contains several cells and the call is handed-off to another cell. This creation/scheduling algorithm enables the *EventList* to stay relatively small; it would not be possible to create and store all the events occurring in the simulation at the start of the simulation.

5.3.4 Organisation of the Simulator

The main class of the software is the class *Simulator*. The *Network* class represents the physical network. A *Network* is made of a number of *Cells*. Each *Cell* manages its resources, by applying CAC policies. Statistics on the number of calls, number of calls blocked, blocking probability, revenue and utility are maintained at the *Cell* level.

The *EventList* stores the different *Events* scheduled during the simulation, ordered by their time of action. The *Output* class is used for managing the averaging over different replications of one scenario and writing results to files.

All simulations parameters are stored in a property file. This includes the duration of the scenario simulated, the number of replications per simulation scenario, the network size, the type of traffic

generated and the behaviour of users. The behaviour of users is specified by their reaction to the price, and the probabilities that they retry to make a call later if the price is too high or their call is blocked. The class *PropertyProvider* provides the methods to read the property files. The class *PropertyLoader* uses this methods to load the different properties into the simulator.

Figure 5.2 presents a simplified class diagram of the organisation of the simulator; a more detailed class diagram can be seen in appendix A.

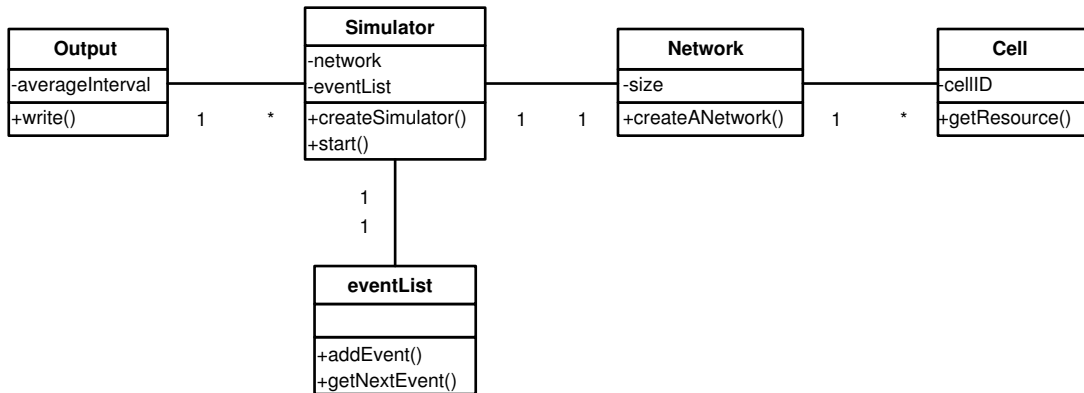


Figure 5.2: Simulator organisation

5.4 Technical Aspects

5.4.1 Generalities

This project has been written in Java, using the J2SE 1.4 and the integrated development tool IntelliJ IDEA 3.0.1. The framework JUnit has been used for automated testing (see section 5.5.1).

5.4.2 Random Number Generation

To generate random numbers the package *cern.jet.random* from the colt distribution [17] has been used. The colt library is an open source library for high performance scientific and technical computing, developed by researchers of the European Organisation for Nuclear Research (CERN). The *cern.jet.random* package provides a large variety of probability distributions featuring high performance generation of random numbers, cumulative distribution functions (CDF) and probability density functions (PDF). This implementation is widely recognised as being reliable and accurate and has been used by several large development projects especially in the area of high performance

numerical analysis (for example in the Scalable Simulation Framework [2]). It has no known bugs. However, to check the correct use of this implementation, all functions used have been extensively tested (see section 5.5.1) prior to their use in this work.

5.4.3 Arrival Rate Modelling

As explained in chapter 3, the call arrival rate is modelled by a Poisson process with a non-stationary rate $\lambda_n(t)$. Generating arrival times $t_1, t_2, t_3\dots$ that follow a non-stationary Poisson process is significantly complex: the first intuition would be to generate t_{i+1} from t_i by generating a variable that follows an exponential distribution of rate $1/\lambda_n(t_i)$ (as, by definition, inter-arrival times of a Poisson process of rate λ follow an exponential distribution of mean $1/\lambda$), however this is not valid, as it would ignore the variation of $\lambda_n(t)$ between t_i and t_{i+1} . Therefore, special care should be given to this task. In the simulator, an algorithm [36] inspired of the *thinning* algorithm presented in [31] has been used. These algorithms work if $\lambda_{max} = \max(\lambda(t))$ is finite. The principle is to generate a stationary Poisson process with a constant rate λ_{max} and arrival times $\{t_i^{max}\}$ and rejecting each t_i^{max} as an arrival with the probability $1 - \lambda(t_i^{max})/\lambda_{max}$. Thus, it is more likely that an arrival time t_i^{max} is accepted if $\lambda(t_i^{max})$ is high, yielding the desired property that arrivals will occur more frequently in intervals for which $\lambda(t)$ is high [36]. The different steps of the algorithm used are the following:

1. Set $t = t_{i-1}$.
2. Generate U_1 and U_2 as two uniformly distributed independent variates.
3. Replace t by $t - (1/\lambda_{max}) \ln(U_1)$.
4. If $U_2 \leq \lambda(t)/\lambda_{max}$, return $t = t_i$. Otherwise, go back to step 2.

5.5 Validation

Building a simulator is an easy task; building a valid and credible simulator is much harder, as every detail of the model chosen need to be implemented and it can be extremely difficult to detect errors. While it is vital to chose an appropriate abstraction model and simulator type, it is also crucial to control the development of the simulator. To this end, several tests and verification procedures have been used in the course of this work, and the simulator has been used to reproduce existing results from previous experiments.

5.5.1 Tests

This simulator has been developed using test-first programming, as this enables a high level of confidence in the resulting system. While defining each function, a test was written for every specific case of the function. The statistical variable generators for each distribution used have also been tested, with a verification of the mean and variance. Moreover each time a generator was used in the simulator, it has been tested that the results were as expected. The use of systematic automatic tests is a crucial factor in the building of such a system, as it avoids numerous errors that may not be easily detected otherwise.

In addition to function testing, several trace analyses have been conducted. These check step by step, by hand calculation, that the system behaviour is correct. Furthermore, the system has been built incrementally, starting with the simplest case and adding features and details, hence simple cases have been tested with different versions of the simulator and the output checked against analytical results.

5.5.2 Results Reproduction

To ensure than the simulator produces valid results, and to perform a complex global test, the five experiments described in [21] have been simulated and the results have been compared with the one given in this article. The similarity of the results produced is a good gage of the validity and accuracy of the simulator written.

5.6 Conclusion

In this chapter, a general overview of the simulator has been presented and the challenging technical aspects detailed. In the following chapter, the experiments run on this simulator and their results will be discussed.

Chapter 6

Experiments and Results

In this chapter, the experiments carried out using the simulator are described. Firstly, the results of simulations using the system in steady state are presented. The results obtained verify the analytical work of Hou, Yang and Papavassiliou. An experiment using the simplified model defined for the mathematical analysis is then presented and the ensuing results are compared with those expected theoretically. In the third section of this chapter, the influence of the system target rate on the revenue and utility is examined and in the following section results obtained using two different hand-off call models are compared. In the next section the impact of the user behaviour model on the efficiency of the pricing scheme is investigated. The final section presents an examination of the behaviour of the pricing scheme for different traffic mixes.

6.1 Steady State

6.1.1 Experiment

The first simulations conducted are in a steady state regime, i.e. with a constant call arrival rate λ_n over a day. The goal is to study the variation in both the total user utility and revenue over a day as a function of λ_n . Apart from the arrival rate, this experiment has the same setting as for the CSwRL experiment carried out in [21] (see section 2.2.3.4): the user behaviour model used is that one third of blocked users leave the system and no pricing scheme is implemented.

6.1.2 Results

The variations of the utility and the revenue as a function of λ_n are shown in figure 6.1. The results given are values got from computing an average taken over 50 simulations. These are then normalised to show the relative variation. It can be seen that there is an optimal value, $\lambda_n = 0.11$ call/s, which maximises the total users utility. This verifies that there is an optimal value for the utility maximisation, as established by Hou, Yang and Papavassiliou. At first sight, this value is quite surprising, as it is significantly different to the value that could have been expected. It might have been expected that this value be equal $\lambda_{cap} = 0.166$, however this difference can be easily explained by the fact that the new call arrival rate is not exactly equal to λ_n but is instead a Poisson process of average arrival rate λ_n , hence the blocking probability tends to be higher. The value of λ_n found differs slightly of the optimal value in steady-state, $\lambda_n = 0.12$ call/s given in [21], but this difference is probably due to small differences in the parameters of the network and the pricing scheme, as the parameters used in [21] are not fully specified. The revenue is continuously growing with λ_n , but converges to an asymptote. This can be explained by the fact that the total traffic admitted over a day is limited by the capacity of the system and that the price is fixed, hence there is a maximal value of the revenue that can be generated over a day.

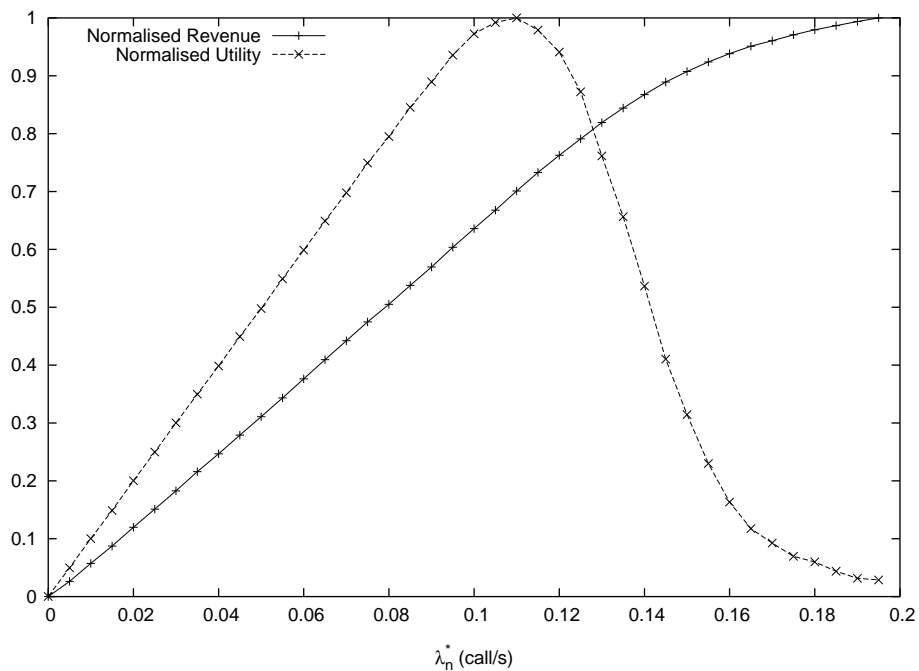


Figure 6.1: Steady state results

6.2 Results Corresponding to the Model Used for the Analytical Analysis

6.2.1 Experiment

For direct comparison with the results of the mathematical analysis presented in chapter 4, an experiment has been run using the traffic model which the mathematical formulae are based on. This model does not include hand-off calls and it is assumed that all blocked users and those who find the price too high leave the system. We study the variation of the total utility and revenue over a day, as a function of λ_n^* .

To obtain comparable results for the case where hand-off calls are included, the total capacity of the system is divided by the ratio of the mean call holding time and the mean cell dwell time, as this is an approximation for the formulae 3.3.1.

6.2.2 Results

The results have been averaged over 100 experiments. Figure 6.2 shows the normalised variation of the total utility and the revenue over a day for different values of λ_n^* (in calls per second). The total utility is maximised for $\lambda_n^* = 0.11$ calls/s whereas the revenue is maximised for $\lambda_n^* = 0.1$ calls/s. This means that a trade-off has to be found between the two maximisation objectives. The value of λ_n^* that optimises the revenue is fairly close to the one expected according to the mathematical analysis. The value of λ_n^* that optimises the total users utility is slightly smaller than the one presented in the mathematical analysis. This may be attributed to the simplifications and assumptions used in the mathematical analysis, as explained in section 4.5.

6.2.3 Conclusion

These results suggest that the mathematical analysis provided accurate results for the simplified models used. Furthermore, as it will be seen in the following sections, these results are quite close to the one of the complete models. The presence of hand-off calls, however, changes slightly the shape of the utility function.

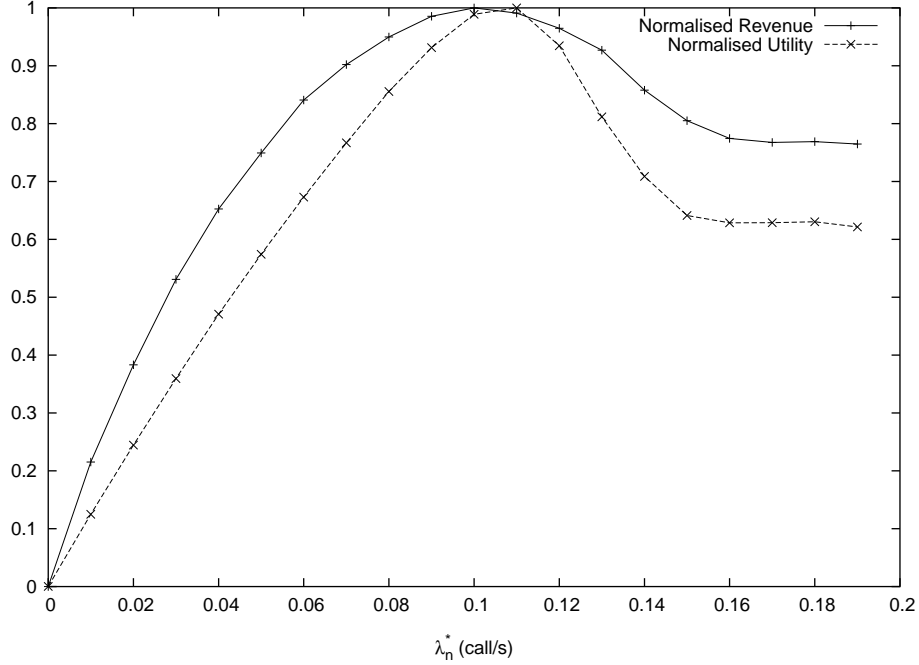


Figure 6.2: Relative variation of utility and revenue with the model used for the mathematical analysis

6.3 Influence of the Target Rate λ_n^*

6.3.1 Experiment

As described in chapter 2, the pricing scheme proposed by Hou, Yang and Papavassiliou in [21] is built around the fact that there is an optimal arrival rate λ_n^* in the system in steady state to maximise the total users utility. Their scheme is designed to regulate the traffic incoming to the call admission block to fit this optimal value. However, as the regulation of the incoming traffic by the price is not perfect, the optimal value to regulate the traffic may be differ from the optimal value in steady state (see section 2.4). The goal of this experiment is to investigate what is the actual optimal value of the regulation rate λ_n^* that maximises the total user utility and if the revenue is maximised at this value.

6.3.2 Results

Figure 6.3 shows the variations of the total users utility and the revenue over a day with λ_n^* . The results have been normalised to show the relative variations. Each scenario corresponds to a different value of λ_n^* and has been replicated 100 times.

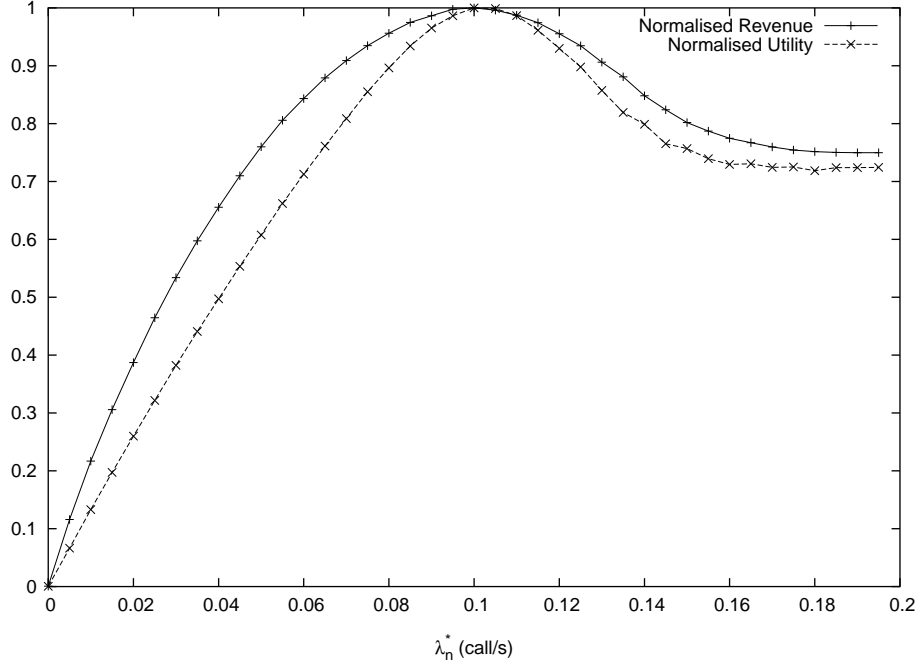


Figure 6.3: Variation of the total users utility and the total revenue over a day with λ_n^*

It can be seen that there an optimal value of λ_n^* to maximise the utility and one to maximise the network operator revenue. This could have been predicted as the total user utility will increase with the number of users admitted to the network, hence with λ_n^* , but after a point the blocking probability will become higher than the limit value P_L and the utility of the admitted users will be zero. Similarly, with the revenue, it will first grow with the number of users admitted to the system, but will then decrease as the fraction of users charged a peak-price will decrease.

It should be noticed than the value of λ_n^* that maximises the total users utility is really close to the one that maximises the network operator revenue. This is due to the fact than the pricing scheme is designed to maximise the total users utility and furthermore that during the simulations, the user behaviour is modelled using the model used for the defining the pricing scheme (this means than the users act exactly as expected).

Furthermore, the optimal value $\lambda_n^* = 0.10$ call/s which maximises the total users utility and the revenue is significantly different than the optimal value in steady state ($\lambda_n^* = 0.11$ call/s). The difference in term of revenue and utility are in the order of approximately 1%. This is not a major difference but is not negligible, especially when considering the revenue.

6.4 Influence of the Hand-off Call Model

6.4.1 Experiments

The goal of these experiments is to compare the results obtained using the two different hand-off call models: modelling and generation by running simulations on several cells (see section 3.3). The simulations run over several cells are run on 19 neighbouring cells, using the wrapped around model.

Two experiments have been carried out: the first one compares the variations of the new call arrival and admission rates and the hand-off call arrival rate during the day for each of the two hand-off models. The second experiment aims to compare the variations of the total users utility and the total revenue over a day with λ_n^* for each model. The settings for all experiments corresponds to those of the PSwRL experiment (see section 2.2.3.4).

6.4.2 Results

Figure 6.4 shows the variation of the new call arrival and admission rates and the hand-off call arrival rate during the day using the two hand-off models. The results are averaged over 10 simulations. It can be seen that the two models are fairly close.

The variation of the total users utility and the total revenue over a day with λ_n^* with the two hand-off models are showed in figures 6.5 and 6.6 respectively. Each scenario has been replicated 10 times. These figures show that the results for the two models are really similar.

6.4.3 Conclusion

The two experiments carried out show that both the results at small scale (every five minutes) and large scale (total for one day) using the two different models for hand-off calls are very similar. This validates the formula used to model the hand-off arrival rate (equation 3.1). As the model using several cells requires significantly more time for each simulation, for other experiments the model with a single cell is used.

6.5 Influence of Call Holding Time Model

6.5.1 Motivations

In Hou, Yang and Papavassiliou's experiments, the call duration (call holding time) is assumed to be independent of the price. They justify this assumption by referring to the practical experiments

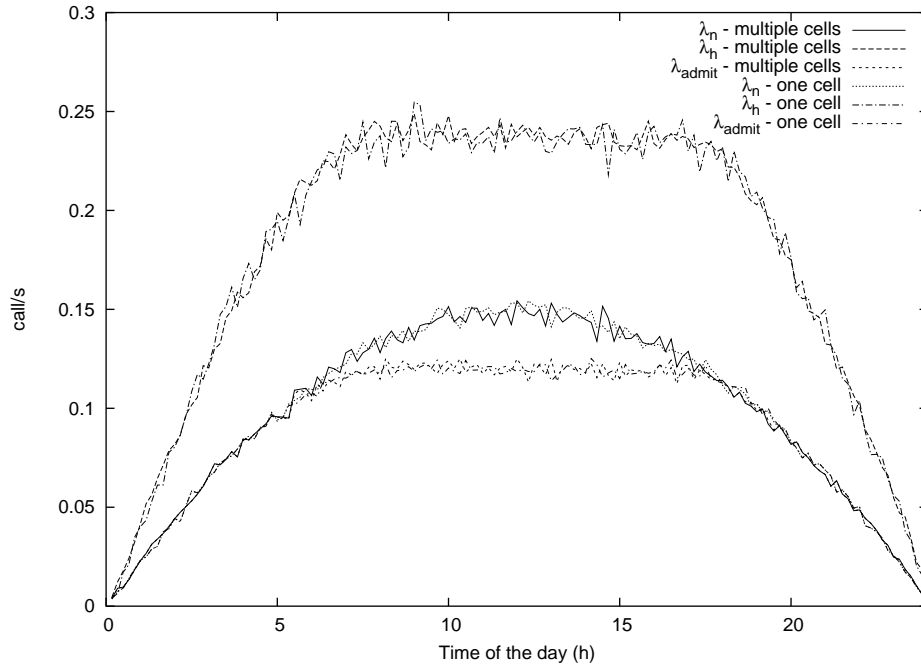


Figure 6.4: Variations of the new call arrival and admission and the hand-off call arrival rate during the day with the two models of hand-off calls studied

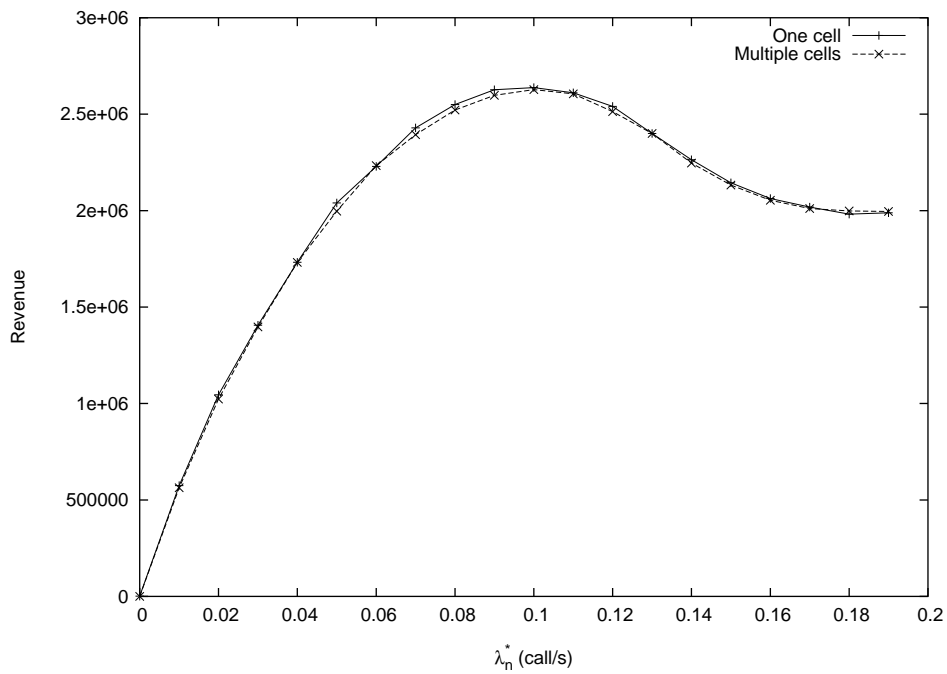


Figure 6.5: Variations of the total revenue over a day in function of λ_n^* with both hand-off models

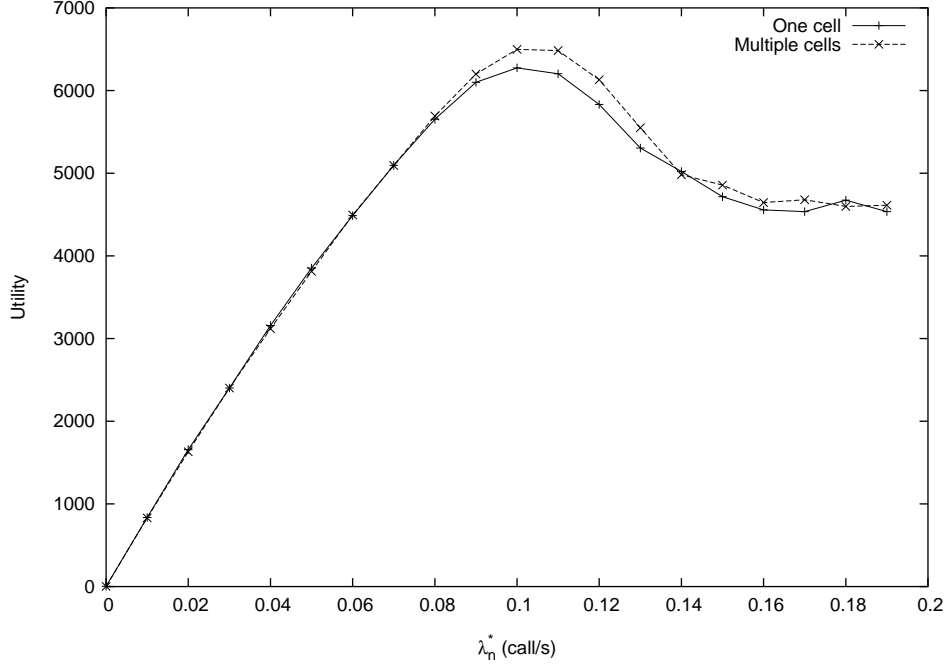


Figure 6.6: Variations of the total users utility over a day in function of λ_n^* with both hand-off models

carried out in [41] (see subsection 2.3.2). However, in the experiments carried out, the price per unit time changes during a call, whereas in [21] a constant price per time unit is used for each call. Therefore the same conclusion may not be applicable.

Furthermore, it seems quite probable that when informed at the beginning of their call that they will be charged a peak price, users will tend to shorten their call duration, and this will depend on the price being charged. For this reason, it has been decided to investigate the influence of the call holding time model on the results of the previous experiments.

6.5.2 Experiment

Four different models of the variation of the average call holding time with price have been studied:

model 0: The average call holding time is independent of price. This is the model used in [21].

$$\tau(p) = \tau_0$$

model 1: The average call holding time is exponentially decreasing with price.

$$\tau(p) = \tau_0 \cdot e^{0.5 \cdot \left(1 - \frac{p}{p_0}\right)}$$

model 2: The average call holding time is exponentially decreasing with price.

$$\tau(p) = \tau_0 \cdot e^{\left(1 - \frac{p}{p_0}\right)}$$

model 3: The average call holding time is exponentially decreasing with the square of price.

$$\tau(p) = \tau_0 \cdot e^{-\left(1 - \frac{p}{p_0}\right)^2}$$

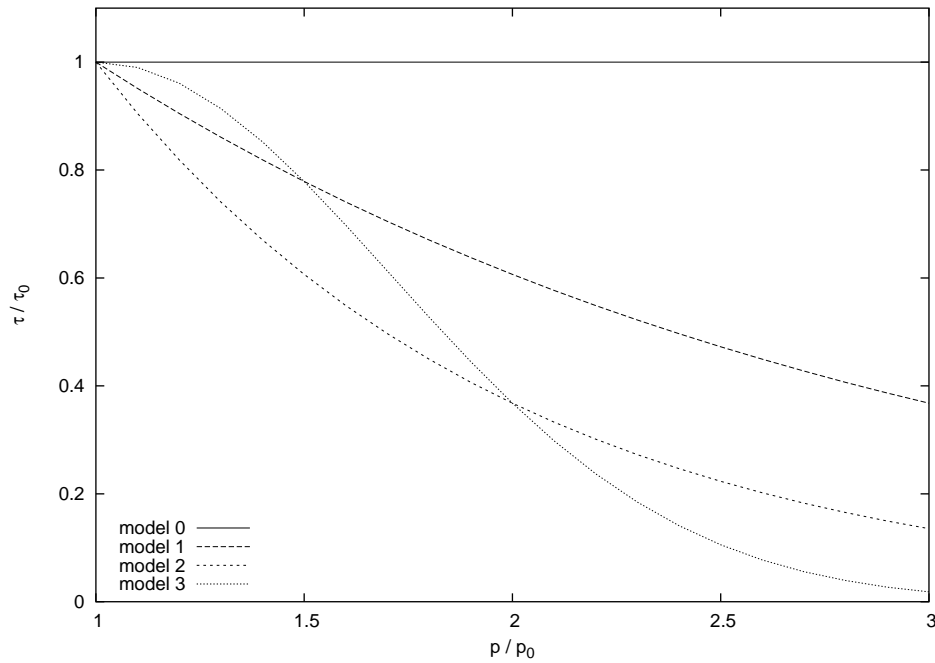


Figure 6.7: Variations of the different call holding time models with the price

Figure 6.7 shows the variations of the different models with price. It must be noted that, for these models, the maximum average call holding time is τ_0 and this decreases as the price increases, hence the total revenue is expected to be smaller with the new models. It has been chosen to study these models as it can be expected that the average call holding time value with an off-peak price is quite well known, whereas less knowledge is available on the reaction of users to price variations. As the utility of one user does not depend on the call-holding time, the total utility will be increased by

these new models, as the number of users admitted will increase when the call holding time decreases.

6.5.3 Results

Figure 6.8 and 6.9 present the variation of the total revenue and utility as a function of λ_n^* for each of the different call holding time models. Each scenario (corresponding to a different value of λ_n^*) has been replicated 10 times.

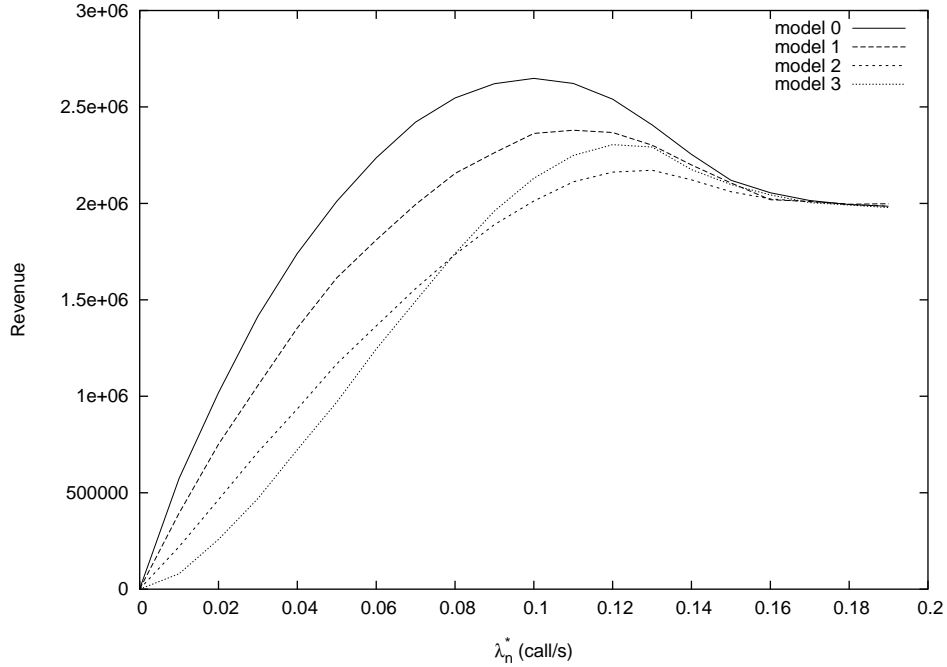


Figure 6.8: Variation in the total revenue over a day as a function of λ_n^* using the different call holding time models

It can be seen from these diagrams that the maximum value of the revenue can be up to 18% less when using one of the alternate models. As for the total users utility, this may be increased by up to 14%. These are significant differences, and while the utility figure does not have any direct meaning in real life, the expected revenue is an important figure for planning the network and tuning the pricing scheme. Furthermore, the optimal values of λ_n^* for maximising the revenue or the utility vary between 0.10 and 0.13 calls per second. This means that a precise model of the user behaviour is required to tune the pricing scheme, as setting λ_n^* to a value other than the optimal one can lead to a significant loss in revenue and utility.

Furthermore, as can be seen in figure 6.10, the optimal values of λ_n^* for maximising the revenue and the utility do no longer coincide. This is most significant for models 2 and 3. In this case, a trade-off

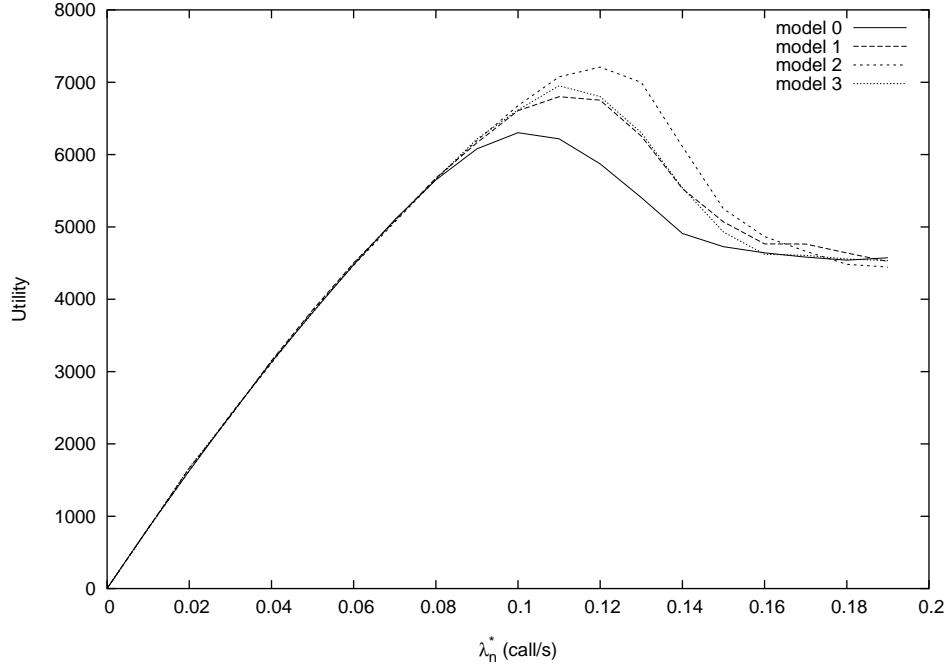


Figure 6.9: Variation in the total users utility over a day as a function of λ_n^* using the different call holding time models

has to be found between maximising the revenue and the utility of users.

6.6 Inclusion of GPRS Traffic

The experiments described in the previous sections have been carried out using GSM traffic only and some improvements to the existing pricing schemes for this traffic have been suggested. In this section, the behaviour of these pricing schemes on different mixes of GSM and GPRS traffic is investigated.

6.6.1 Experiments

The GPRS traffic used by the simulator is generated using an implementation of the GPRS model described in chapter 3. The behaviour of the pricing scheme for three different types of traffic mixes is examined. The first scenario is the one described previously and contains only GSM traffic. The second scenario contains only GPRS traffic and the third scenario contains one third GPRS and two thirds GSM traffic. Each scenario has been replicated 10 times.

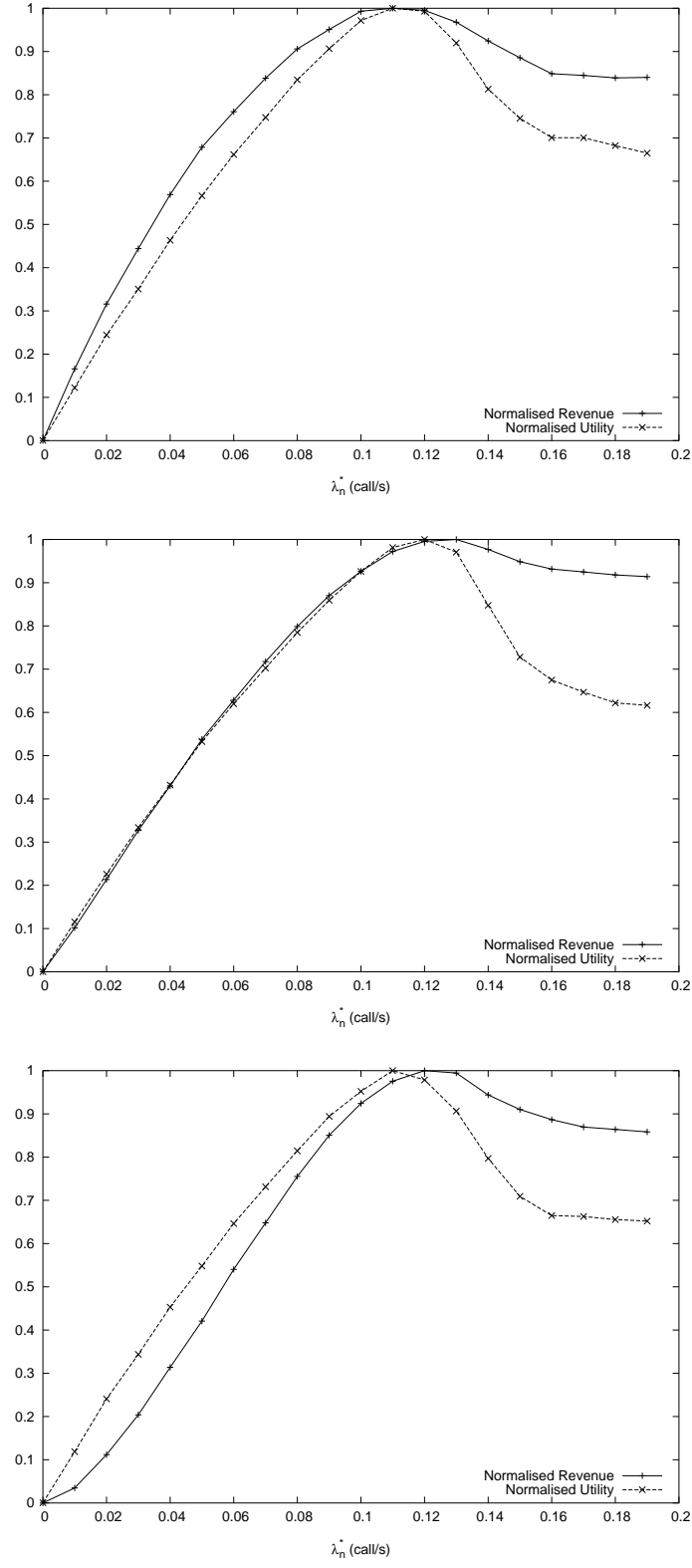


Figure 6.10: Variations of the revenue and the total users utility as a function of λ_n^* for the call-holding time model 1 (top), model 2 (centre) and model 3 (bottom)

According to the GPRS traffic model described in chapter 3, the mean session duration of GPRS traffic is significantly higher than the mean call holding time for GSM traffic. This means that for the same traffic volume in the system, less GPRS calls are admitted. Hence the pricing scheme has been adapted by sizing the value of the target arrival rate by the ratio of the two mean durations, so that the traffic scheme will have similar effect on both types of traffic.

6.6.2 Results

As the total utility function, defined in section 4.4.3, is not dependent on the duration of the calls, but rather on the number of calls admitted, the total utility will be significantly smaller for GPRS traffic. This is demonstrated in figure 6.11, which shows the total utility for each of the scenarios. This figure also shows that for the mix of both GPRS and GSM traffic, the total utility reaches a steady state instead of declining from a maximum as for the other scenarios. The revenue generated by each of the schemes is shown on figure 6.12. It can be seen that the revenue is lower for single type traffic mixes. This is due to the fact that there are two separate prices for the two traffic types, and that they will not increase as much if there are less traffic of their type.

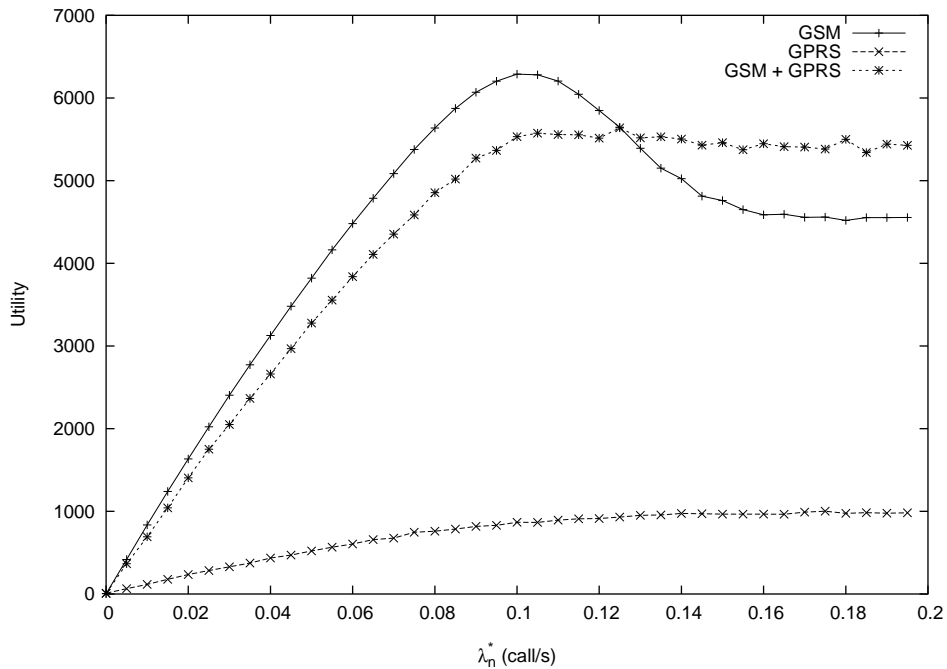


Figure 6.11: Comparison of the utility for each of the traffic mixes

Figure 6.13 shows the normalised variation of the revenue and the utility for each of the scenarios. It can be seen that if the pricing scheme provides a single value of target incoming rate for optimising

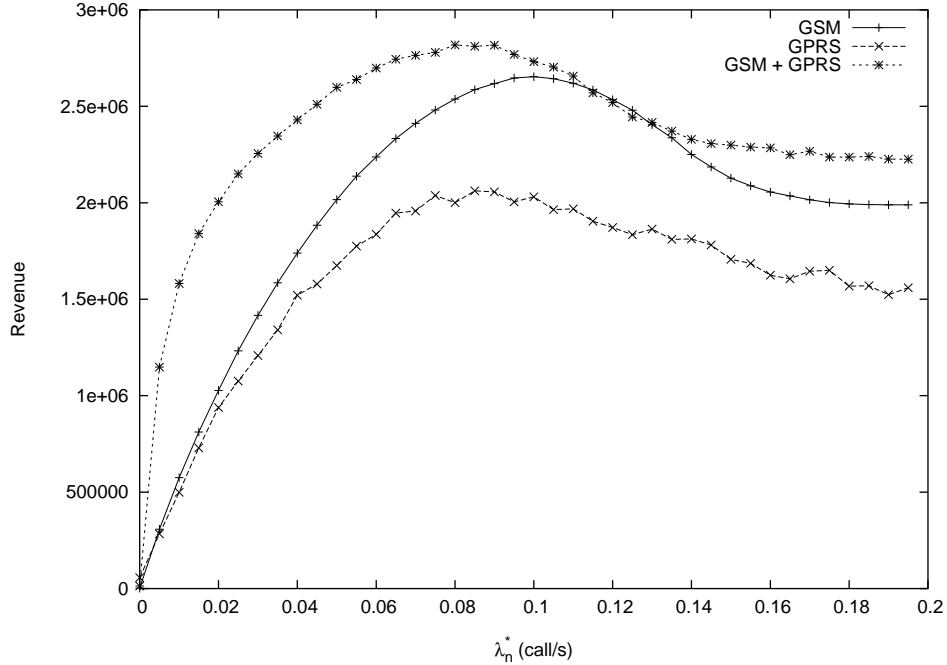


Figure 6.12: Comparison of the revenue for each of the traffic mixes

both revenue and utility in the case of GSM traffic, then this is not automatically the case when GPRS traffic is included. Therefore the pricing scheme should be refined to take into account the features of GPRS traffic.

6.7 Conclusion

In this chapter, the experiments carried out to test existing pricing schemes using the traffic and network models created have been presented. These suggest that care should be put into the choice of the target incoming traffic rate, and that a detailed knowledge of the demand and the reaction of users to price and QoS variations are required to design an efficient pricing scheme.

Furthermore, the inclusion of GPRS traffic outlines the need to defining a new utility function that would take into account the duration of calls, as this is an important parameter to measure the service given to users. It also shows that pricing schemes defined for GSM cannot be used directly for GPRS traffic, as any optimisations carried out for GSM networks do not automatically apply to GSM/GPRS ones.

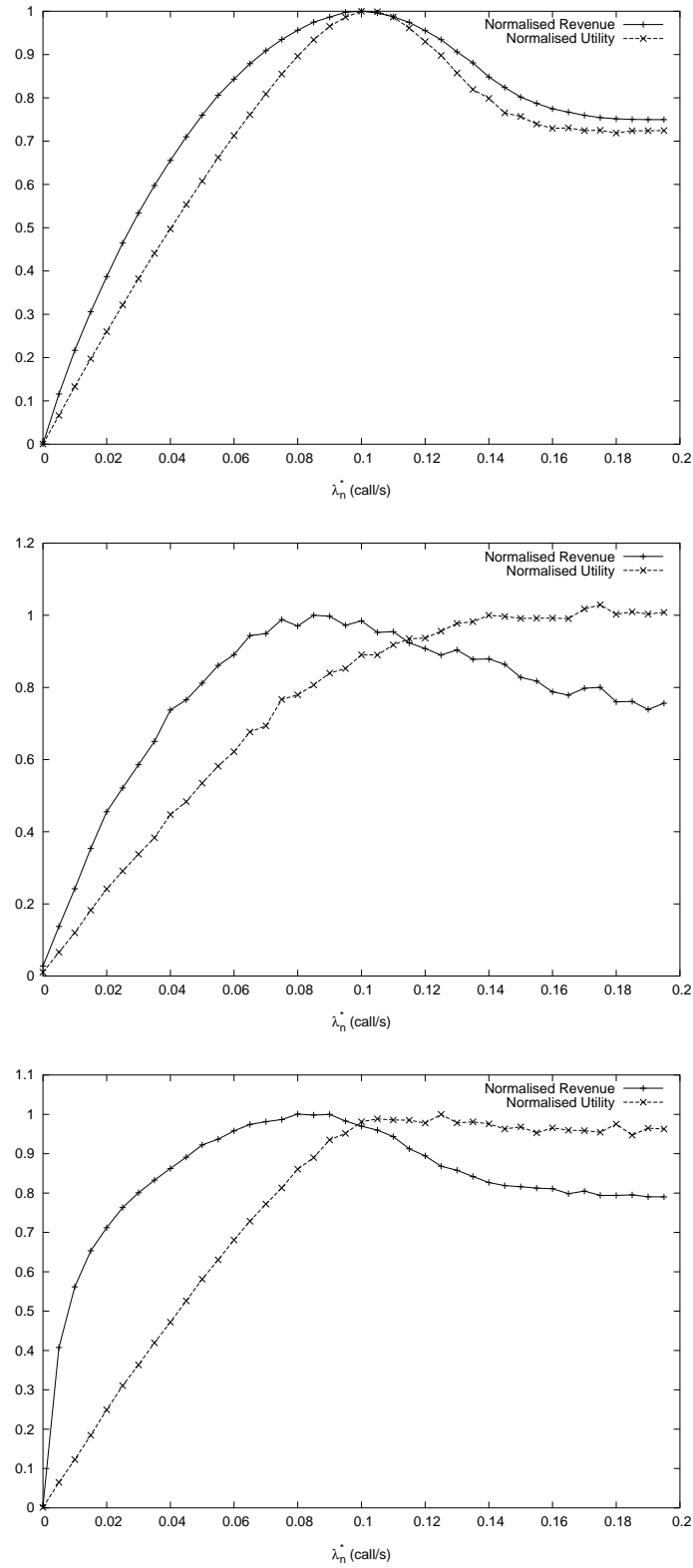


Figure 6.13: Variation of the revenue and the total utility as a function of λ_n^* for the three scenarios: pure GSM (top), pure GPRS (centre), mix GSM/GPRS (bottom)

Chapter 7

Conclusions

The goal of this project was to investigate dynamic pricing in cellular networks. As explained in chapter 2, only a few studies have been conducted on dynamic pricing in cellular networks. While thorough studies of dynamic pricing in fixed network have been carried out, the mobility of users makes the study of pricing in cellular networks much more complex. Furthermore, the exact nature of future networks and their usage are as yet unknown, hence there is no precise model of user behaviour. The goal of this work was to model, in detail, existing networks and to conduct a thorough investigation of their behaviour.

This work combines the principal features of two main studies on dynamic pricing in cellular networks, that is it combines the pricing scheme with call admission control as introduced by Hou, Yang and Papavassiliou and it introduces GPRS traffic as in the work of Fitkov-Norris and Khanifar. In the pricing scheme proposed by Hou, Yang and Papavassiliou, it was shown that there is an optimal new call arrival rate which maximises the total users utility when the system is in steady state. The pricing scheme aims to make the system arrival rate fit this optimal rate. However it was noticed that the optimal target rate could differ from the optimal arrival rate in steady state, therefore it was decided to explore how the total users utility and the revenue over one day would vary in function of this target rate.

7.1 Achievements

First a mathematical analysis of a simplified model has been carried out. This analysis gave a deeper insight into the pricing scheme proposed by Hou, Yang and Papavassiliou. Analytical expressions for both the total users utility and the revenue have been established. However, the simplifications

and assumptions of this mathematical analysis mean that it is not a completely accurate model, and hence the validity of the results could be open to question.

For this purpose, a simulator has been written. This uses a complex and detailed model of the network and standardised traffic models. Therefore, the simulator constitutes a powerful tool for the performance analysis of pricing schemes.

Using this simulator, the result derived analytically by Hou, Yang and Papavassiliou that there exists an optimal constant arrival rate for maximising the utility of all users has been verified. Furthermore, the specific value of this optimal arrival rate for the system modelled has been found. Simulations using the simplified traffic and network models used for the mathematical analysis were conducted. The results concerning the utility were significantly different from those expected. This may be attributed to the assumptions used in the mathematical analysis. Results for the revenue were quite similar to those predicted by the model.

An experiment to investigate if the optimal target rate for new call arrivals to the system was equal to the optimal arrival rate in steady state was conducted. It was found that there was a significant difference between these two values, even if the difference in the corresponding values of utility and revenue is not very large.

In the study of Hou, Yang and Papavassiliou, the hand-off call arrival rate in the cell has been computed using an analytical formula. The validity of this formula had not been shown theoretically, hence experiments were run to compare the results given by this model with those obtained by running simulations on several cells, with calls actually being handed-off between cells. To avoid the border effect in the latter model, the cells have been wrapped around. The results of the simulations using the two models are very similar on both a small and large time scale.

The next experiment carried out related to the modelling of the call holding time. Hou, Yang and Papavassiliou assumed that the call holding time is independent of price. As it seems quite plausible that the users would tend to reduce their call holding time when the price is too high, several models for the variation of call holding time with price have been studied. Between these models, the results differ significantly both in term of optimal value of the target rate and maximal value of revenue and utility. Furthermore, the network operator revenue can be significantly reduced when the reaction of users is not exactly as expected by the pricing scheme definition. This suggests that an accurate and detailed knowledge of the demand is a crucial element in the design of an effective pricing scheme.

The last experiment was to include GPRS traffic. The results of this experiment show that pricing schemes defined for GSM traffic are not as efficient when they are applied to other types of traffic. This is mostly due to differences in the average duration of GPRS traffic session: as GPRS sessions are on average significantly longer than GSM calls, hence the regulation by the price is less efficient. This

needs to be taken into account while designing any future pricing scheme for combined GSM/GPRS networks.

To investigate the effects of dynamic pricing in cellular networks, a simulator has been written. With this simulator, an existing model of hand-off calls has been validated and it has been shown that an existing pricing scheme could be improved, by changing the value of the target rate. Furthermore, the importance of a complete and accurate model for the demand has been established. This last conclusion suggests that future studies should be directed towards more detailed modelling of users behaviour; one possible solution would be to segment users into classes, with different QoS requirements and reactions to price change as has been done in fixed networks. Also, the exact traffic mix expected in the network should be thoroughly investigated, as this plays an important role in the design of a pricing scheme.

7.2 Obstacles Overcome

One of the main difficulties encountered was the definition of the network model: several of the aspects of cellular networks are not standardised, hence significant work was required to study the existing literature and identify the most recognised and promising schemes, and to model them. Much effort has also been directed towards studying different users behaviour models so as to identify the most appropriate one for this study. Another difficult task was to assimilate the work carried out on dynamic pricing in cellular network and in other fields.

To define the type of simulator required and the features needed, and to ensure that the simulator would be credible and accurate, a survey of existing simulators and simulation methodologies was conducted. It was also necessary to identify accurate tests to ensure that the behaviour of the simulator was as expected and that it was bug free.

Finally, the task of defining meaningful experiments and appropriate scenarios for each of these experiments together with the running of these experiments proved extremely time-consuming.

7.3 Future Work

Two main types of traffic, GSM and GPRS have been studied. However, for GPRS traffic, only web browsing traffic has been considered. An interesting extension to this work would be to use a more complete description of GPRS traffic, by taken into account other possible uses, for example e-mail and video-telephony. Another direction for future work would be to test the behaviour of different pricing schemes using the simulator and compare their behaviour using different demand models and

traffic mixes. A more theoretical extension would be to broaden the mathematical analysis and to conduct a deeper theoretical study to define a new pricing scheme using the detailed model presented in this work. The performance of any such pricing scheme could then be tested using the simulator.

Appendix A

Complete Class Diagrams

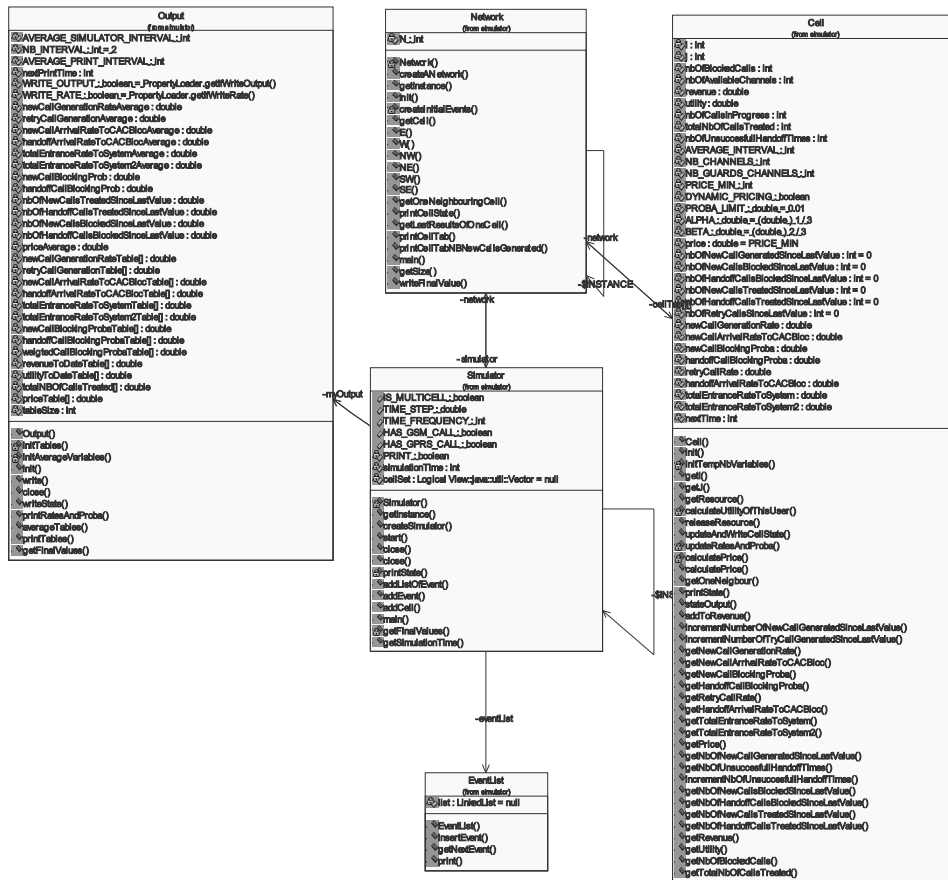


Figure A.1: Simulator organisation: detailed class diagram



Figure A.2: Different types of events: detailed class diagram

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